

Total No. of Questions : 6]

SEAT No. :

P3969

[Total No. of Pages : 2

[4860] - 35

M.E. (Civil) (Structures) (Semester - I)
ADVANCED SOLID MECHANICS
(2008 Pattern)

Time : 4 Hours]

[Max. Marks : 100

Instructions to the candidates:

- 1) Answer any two questions from each section.*
- 2) Answer to the two sections must be written in separate books.*
- 3) Neat diagrams must be drawn wherever necessary.*
- 4) Figures to the right indicate full marks.*
- 5) Use of electronic pocket calculator is allowed.*
- 6) Assume suitable data, if necessary.*

SECTION - I

- Q1)** a) What is compatibility of strains? Obtain strain compatibility equation for 2D problem in elasticity? **[10]**
- b) A plane passing through point (x, y, z) in a stressed elastic body has its normal 'n' with direction cosines $\cos(n, x)$, $\cos(n, y)$, $\cos(n, z)$. Obtain expressions for the stress resultants (T_n) and its direction in terms of six independent components at that point. **[15]**
- Q2)** a) State and explain the Generalized Hook's Law. Hence obtain the Lamé's constants and engineering constants for an elastic isotropic body. **[7]**
- b) Define Airy's stress function ' Φ '. Prove that the stress function satisfies the Biharmonic Governing Equation in absence of body forces. **[8]**
- c) If Φ is a second degree polynomial function, obtain the stress distribution on the sides of rectangular plate of size $L \times 2h$. Neglect body forces. Also check for static equilibrium of the plate under this stress distribution. **[10]**

P.T.O.

- Q3)** a) Explain the concept of Stress Invariants. Hence, discuss the state of pure shear and hydrostatic state of stress. [7]
- b) Obtain the solution for stress distribution σ_r and σ_θ in a hollow cylinder subjected to uniform external pressure ' P_o ' and internal pressure P_i ? [8]
- c) Find stress components of a cantilever beam loaded with point load at the free end by using Airy's stress function polynomial? [10]

SECTION - II

- Q4)** a) What is axi-symmetric problem? Write the compatibility equation and corresponding stress components by assuming suitable solution? [7]
- b) A thick cylinder of internal radius 120mm and external radius 175 mm is subjected to an internal pressure of 10 N/mm². Determine variation of radial and hoop stresses in the cylinder wall? [8]
- c) Using polar co-ordinates, obtain the solution for stress distribution for radial and transverse stresses if there is a circular hole of radius 'a' inside an infinite elastic medium and subjected to internal pressure ' P_i '. [10]
- Q5)** a) Derive Poisson's equation for torsion of prismatic bars of non-circular section in terms of stress function Φ using St. Venants Theory. Neglect body forces. [15]
- b) A shaft of elliptical c/s having semi major axis 75mm and semi minor axis 25 mm is subjected to a torque of 1 kN-m, determine maximum and minimum shear stress developed in shaft. [10]
- Q6)** a) Derive differential equation for the elastic line of a beam resting on an elastic foundation. [10]
- b) A semi infinite beam is subjected to a force ' P ' and a moment ' M_o ' at one end. Starting from the solution for an infinite beam, obtain the solution at a section ' z ' from the beam end for [15]
- i) Deflection ' y '.
- ii) Bending moment M_x .

