Total N	o. of Q	uestions	:	12]
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SEAT No. :	:[		
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P1418 [4858] - 185

## T.E. (Computer Engg.) THEORY OF COMPUTATION

(2008 Pattern) (Semester - I)

Time: 3 Hours [Max. Marks: 100

## Instructions to the candidates:

- 1) Answer question 1 or 2, 3 or 4 and 5 or 6 from Section I and question 7 or 8, 9 or 10 and 11 or 12 from Section II.
- 2) Answers to the two sections should be written in separate answer books.
- 3) Neat diagrams must be drawn wherever necessary.
- 4) Figures to the right indicate full marks.
- 5) Assume suitable data if necessary.

## **SECTION - I**

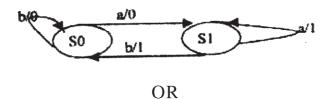
*Q1*) a) Define the following terms.

[6]

- i) Kleen Closure
- ii) Finite Autimata
- iii) Transition Diagram
- b) Design DFA for a language of string 0 & 1 that

[6]

- i) Ending with 11
- ii) Either begin or end with 01
- c) Convert the following Mealy Machine to Moore Machine. Show the output for input string 'abba' through Moore machine. [4]



Q2)	a)	Convert	DFA	to	NFA.
~	/				

	0	1
p	{p,q}	{p}
q	{r}	{r}
r	{s}	φ
s*	{s}	{s}

b) Design a Moore Machine that gives an output of 1 if the input string ends in 'bab'. Convert the same Moore Machine to Mealy Machine.

[8]

[4]

[8]

Q3) a) Show 
$$((a+bb)*aa)*$$
 and  $\epsilon+(a+bb)*aa$  are equivalent.

b) Prove that 
$$(1+00*1)+(1+00*1)(0+10*1)*(0+10*1)=0*1(0+10*1)*$$

c) Convert following Regular Expression to DFA (Regular Expression to NFA with  $\epsilon$  moves and direct method to convert NFA with  $\epsilon$  to DFA) [8]

$$R.E.=01[(10*+111)*+0]*1$$

OR

**Q4)** a) Show for regular expression 
$$(rs+r)*r=r(sr+r)*$$

b) Draw DFA of following Regular Expression. [6]

i) 
$$(11+00)$$
\*

c) Using pumping lemma show that the language  $L=\{a^mb^n | m>n\}$  is not regular. [6]

[6]

[4]

$$E \rightarrow E + T | T$$

$$T \rightarrow T*F|F$$

$$F \rightarrow (E) \mid a \mid b$$

Give derivation of (a+b)\* a+b using sentential form and parse tree

b) Give context free grammar for following.

[6]

i) 
$$(011+1)*(01)*$$

ii) 
$$0^{i}1^{i+k}0^{k}$$
 where i,  $k > 0$ 

[6]

$$S \rightarrow ASB \mid \epsilon$$

$$A \rightarrow aAS \mid a$$

Q6) a) Construct the right linear grammar corresponding to the regular expression.[6]

R=(0+1)1\*(1+(01)\*)

b) Discuss the following applications of CFG.

**[6]** 

[6]

- i) Parser
- ii) Markup Languages
- c) Convert the grammar given below to its equivalent CNF.

 $S \rightarrow PQP$ 

P→0P | ε

 $Q\rightarrow 1Q \mid \epsilon$ 

## **SECTION - II**

Q7) a) Construct a PDA equivalent to the following.

[8]

CFG G.

 $S \rightarrow OBB$ 

 $B \rightarrow OS \mid 1S \mid 0$ 

Test whether  $.010^4$  is in N(A).

b) Define acceptance by PDA.

**[4]** 

- i) By final state
- ii) By empty stack
- c) Construct pushdown automata  $L = \{W \subset W^R | W \in (a + b)^*\}$  and  $W^R$  is reverse string of W. [6]

OR

Q8) a) Consider the PDA with following moves. Construct a CFG equivalent to PDA.[8]

 $M = (\{q_0, q_1\}, \{a, b\}, \{P, Z_0\}, \delta, q_0, Z_0, \phi)$  and  $\delta$  is given as :

$$\delta(q_0, a, Z_0) = (q_0, PZ_0)$$

$$\delta(q_0, a, P) = (q_0, PP)$$

$$\delta(q_0, b, P) = (q_1, \epsilon)$$

$$\delta(q_1, b, P) = (q_1, \epsilon)$$

$$\delta(q_1, \epsilon, P) = (q_1, \epsilon)$$

$$\delta(q_1, \epsilon, Z_0) = (q_1, \epsilon)$$

- b) Compare deterministic PDA with non-deterministic PDA. [4]
- c) Obtain a PDA to accept the language  $L = \{a^nb^n \mid n \ge a\}$  by final state.

**[6]** 

Q9)	a)	and TM. [8]			
	b)	Design a turing machine M to recognize the language $\{a^nb^nc^n\mid n\geq 1\}$	[ } <b>8]</b>		
		OR			
<b>Q10</b> ) a)		Write short notes on:	8]		
		i) Universal Turing Machine.			
		ii) Composite Turing Machine.			
		iii) Iterated Turing Machine.			
		iv) Multitape Turing Machine.			
	b)	Design a turing machine for finding.2's complement of a binumber.			
	c)	Construct a post machine for the language $L = \{0^n1^n \mid n \ge 0\}$	4]		
Q11)	a)	Describe in detail Chomsky Hierarchy with example. [8]	8]		
1 2		Show that if $L_1$ & $L_2$ are recursively enumerable languages over then $L_1 \cup L_2$ and $L_1 \cap L_2$ are also recursively enumerable. [8]	Σ <b>8]</b>		
		OR			
<b>Q12</b> ) a)		Define the following terms:	8]		
		i) Post correspondence problem			
		ii) Un-decidability			
		iii) Context sensitive language			
		iv) Recursive & Recursively Enumerable language			
	b)	What is Halting problem? Prove that halting problem is undecidabl  [8]	e. 8]		

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