

[4858] - 160

T.E. (Electronics)

**Discrete Time Signal Processing
(2008 Pattern) (Semester - II)**

Time : 3 Hours]

[Max. Marks : 100

Instructions to the candidates:

- 1) *Answer any three question from each section.*
- 2) *Answers to the two sections should be written in separate books.*
- 3) *Neat diagrams must be drawn wherever necessary.*
- 4) *Figures to the right indicate full marks.*
- 5) *Use of logarithmic tables, slide rule, Mollier charts, electronic pocket calculator and steam tables is allowed.*
- 6) *Assume suitable data, if necessary.*

SECTION - I**Q1)** a) An analog signal is given by [6]

$$x(t) = 3 \cos 100 \pi t + 2 \sin 300 \pi t - 4 \cos 100 \pi t$$

- i) What is the Nyquist rate for this signal?
 - ii) Write the equation of sampled signal.
 - iii) If the signal is sampled at a rate of 200 sam/sec. What is the discrete time signal obtained after sampling?
- b) What are the advantages of discrete time signal processing over analog signal processing? [6]
- c) Explain Direct form II structures for realization of LTI discrete time systems. [6]

OR

Q2) a) Discrete time systems $h_1(n)$ & $h_2(n)$ are connected in cascade. [6]

$$h_1(n) = \left\{ \frac{1}{2} \quad \frac{1}{4} \quad \frac{1}{2} \right\} \quad h_2(n) = \delta(n - 2)$$

Determine the response of the overall system to the input

$$x(n) = \delta(n + 2) + 3\delta(n - 1) - 4\delta(n - 3)$$

P.T.O.

- b) A difference equation of discrete time system is given below : [6]

$$y(n) - \frac{2}{5}y(n-1) + \frac{3}{7}y(n-2) = 2x(n) + \frac{2}{3}x(n-1)$$

Draw direct form I & direct form II structures.

- c) Determine the impulse response of the systems described by the difference equation. [6]

$$y(n) = 0.6y(n-1) - 0.08y(n-2) + x(n)$$

- Q3)** a) Compute the 4 - point DFT of the following sequence $x(n) = \{1 \ 1 \ 1 \ 1\}$. [4]

- b) Compute the circular convolution of the following sequences. [4]

$$x_1(n) = \{4 \ 3 \ 2 \ 1\} \quad x_2(n) = \{1 \ 2 \ 1 \ 2\}$$

- c) Explain the following properties of DFT. [8]

- i) Linearity
- ii) Time shifting
- iii) Circular convolution

OR

- Q4)** a) Compute the 8-point DFT of the following sequence using DIT FFT algorithm. [10]

$$x(n) = \{1 \ 2 \ 2 \ 1 \ 1 \ 2 \ 1 \ 1\}$$

- b) Find IDFT of the following sequence. [6]

$$x(k) = \{7 \ -2-j \ 1 \ -2+j\}$$

- Q5)** a) State and explain the condition of causality and stability of the discrete time system. [6]

- b) Compute the z-transform of [10]

i) $x_r(n) = \left(\frac{1}{2}\right)^n u(n) + (3)^n u(-n-1)$

ii) $x_r(n) = a^{|n|}$

iii) $x(n) = n(a)^n u(n)$

OR

Q6) a) Compute the z-transform of [4]

$$x(z) = \frac{1}{1 - 1.5z^{-1} + 0.5z^{-2}}$$

for i) ROC : $|z| > 1$ ii) ROC : $|z| < 0.5$

b) Determine the impulse response of the system. [6]

$$H(z) = \frac{1 - z^{-1}}{1 - 0.2z^{-1} - 0.15z^{-2}}$$

c) Sketch the following sequences. [6]

compute z - transforms

plot pole zero plots for following sequences

i) $x(n) = (1)^n u(n)$ ii) $x(n) = (-1)^n u(n)$

SECTION - II

Q7) a) Convert the analog filter with system function [5]

$$H_a(s) = \frac{s + 0.1}{(s + 0.1)^2 + 9}$$

into digital IIR filter by means of Bilinear transformation. The digital filter should have resonant frequency of $\omega_r = \pi/4$.

b) Explain frequency warping in Bilinear transformation. What are the advantages of Bilinear transformation over Impulse Invariance transformation? [5]

c) Design a single pole low pass digital filter with a 3-dB bandwidth of 0.2π using bilinear transformation applied to the analog filter. [8]

$$H(s) = \frac{\Omega_c}{s + \Omega_c}$$

where Ω_c is 3-dB bandwidth of analog filter. Also compute the magnitude at $\omega = 0$ & $\omega = 0.2\pi$.

OR