Total No. of Questions—8]

[Total No. of Printed Pages—4+1

Seat No.

[4957]-1071

## S.E. (Computer) (First Semester) EXAMINATION, 2016

## DISCRETE STRUCTURES

## (2012 **PATTERN**)

Time: Two Hours

Maximum Marks: 50

**N.B.** :— (i) Neat diagrams must be drawn wherever necessary.

- (ii) Figures to the right indicate full marks.
- (iii) Assume suitable data, if necessary.
- **1.** (a) Use mathematical induction to show that :

$$1^{2} - 2^{2} + 3^{2} - 4^{2} + \dots + (-1)^{n-1} n^{2} = (-1)^{n-1} \cdot \frac{n(n-1)}{2}.$$
 [4]

- (b) The converse of statements is given. Write inverse and contrapositive statements. [3]
  - (i) If he is considerate of others, then a man is a gentleman.
  - (ii) If a steel rod is stretcher, then it has been heated.
- (c) Use Warshall's algorithm to compute the transitive closure of  $R \cup S$  for the relations R and S defined on  $A = \{1,2,3,4\}$  described as:

$$\mathbf{M}_{R} = \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}, \quad \mathbf{M}_{S} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}$$

- **2.** (a) Let A and B be sets such that  $(A \cup B) \subseteq B$  and  $B \not\subset A$ . Draw the corresponding Venn diagram. [3]
  - (b) Among 100 students, 32 study mathematics, 20 study physics, 45 study biology, 15 study mathematics and biology, 7 study mathematics and physics, 10 study physics and biology and 30 do not study any of the three subjects. [6]
    - (i) Find the number of students studying all three subjects.
    - (ii) Find the number of students studying exactly one of the three subjects.
  - (b) Let R and S be two relations whose corresponding diagraphs are shown in fig 2.1, Compute: [4]
    - (i) R<sup>-</sup>
    - (ii) R  $\cap$  S
    - (iii) R  $\cup$  S
    - (iv) S<sup>-1</sup>.

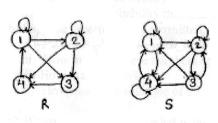


Fig. 2.1

3. (a) Consider the Binary operation \* on Q, the set of rational numbers defined by a \* b = a + b - ab,  $\forall a, b \in Q$ . Determine whether \* is group. [6]

(b) Use Dijkstra's algorithm to find the shortest path between a and z for Fig. 3.1. [6]

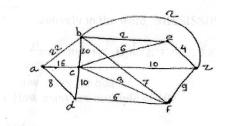


Fig. 3.1.

Or

- 4. (a) Show that (F, +, .) is a field where F is set of all rational numbers and + and are ordinary addition and multiplication operations. [6]
  - (b) Use nearest neighbour method to find the Hamiltonian circuit starting from 'a' in the Fig. 4.1, find its weight. [6]

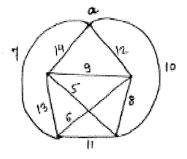


Fig. 4.1

[6]

- **5.** (a) Define the following terms with example :
  - (i) Binary search tree
  - (ii) Bipartite graph
  - (iii) M-ary tree.

(b) For the following sets of weights, construct an optimal binary prefix code for each weight in the set, give the corresponding code word: 8, 9, 10, 11, 13, 15, 22. [7]

Or

6. (a) Give the stepwise construction of minimum spanning tree using Prim's algorithm for the graph in Fig. 6.1. Obtain the total cost of minimum spanning tree. [7]

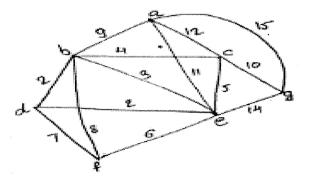
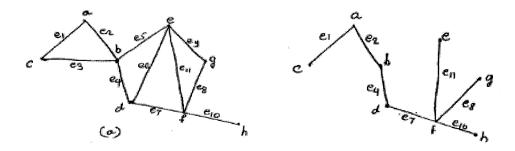


Fig. 6.1.

(b) Find the fundamental system of cut-set for the graph G shown below with respect to the spanning tree T. [6]



- 7. (a) (i) If the letters of the word 'REGULATIONS' be arranged at random. What is the chance that there will be exactly 4 letters between R and E?
  - (ii) What is the probability that four S's come consecutively in the word 'MISSISSIPPI'?
  - (b) Suppose repetitions are permitted: [6]
    - (i) How many ways three digit number can be formed six digits 2,3,4,5,7 and 9 ?
    - (ii) How many of these numbers are less than 400 ?
    - (iii) How many are even?
    - (iv) How many are odd?
    - (v) How many are multiple of 5 ?
    - (vi) How many are multiple of 10 ?

Or

- **8.** (a) If two dice are thrown, what is the probability that the sum is:
  - (i) Greater than 8 ?
  - (ii) Neither 7 nor 11 ?
  - (b) Four persons are chosen at random from a group containing 3 men, 2 women and 4 children. Find the chance that exactly two of them will be children. [6]