

[5058] - 165

T.E. (IT)

THEORY OF COMPUTATION

(2008 Course) (Semester - I)

Time : 3 Hours]

[Max. Marks :100

Instructions to the candidates:

- 1) Solve Q.1 or Q.2, Q.3 or Q.4, Q.5 or Q.6 from the SECTION I.*
- 2) Solve Q.7 or Q.8, Q.9 or Q.10, Q.11 or Q.12 from the SECTION II.*
- 3) Answers to the two sections should be written in separate answer books.*
- 4) Neat diagrams must be drawn wherever necessary.*
- 5) Assume suitable data if necessary.*

SECTION - I

- Q1)** a) Design FA/FSM accept only those strings which ending with “abb” over input = {a, b} [8]
- b) Define and explain: [6]
- i) Alphabet and Strings.
 - ii) Formal Language.
 - iii) Regular expression.
- c) Show that $(0 + 1)^* = (0^* 1^*)^*$ [4]

OR

- Q2)** a) Design a finite automata which perform addition of two Binary number.[8]
- b) Give RE for following language over = {0, 1} [6]
- i) The language of all strings containing exactly two 0's.
 - ii) The language of all strings containing at least two 0's.
 - iii) The language of all strings not containing the substring 00.
- c) Define Finite State Machine. Explain its properties and limitations. [4]

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- Q3)** a) Design a Mealy machine to check divisibility of decimal number by 4. [8]
 b) Construct DFA for regular expression $(0 + 1)^*$, $(00 + 11)$. [8]

OR

- Q4)** a) Construct a NFA and its equivalent DFA for accepting a language defined over input = $\{0, 1\}$ such that each string has two consecutive zeros followed by 1. [8]
 b) Construct NFA with epsilon move for the following regular expression. [8]
 i) $(00 + 1)^* (10)^*$
 ii) $10 + (0 + 11) 0^* 1$

- Q5)** a) Consider the following grammar [6]

$S \rightarrow aB \mid bA,$

$A \rightarrow a \mid aS \mid bAA,$

$B \rightarrow b \mid bS \mid aBB$

Derive the string aaabbb using

- i) Leftmost derivation.
 ii) Rightmost derivation.
 b) Convert the following grammar to Chomsky Normal Form (CNF) [6]
 $S \rightarrow AACD$
 $A \rightarrow aAb \mid \epsilon$
 $C \rightarrow aC \mid a$
 $D \rightarrow aDa \mid bDb \mid \epsilon$
 c) Construct context free grammar corresponding to regular expression. [4]
 $(0 + 1) 1^* (1 + (01)^*)$

OR

- Q6)** a) Write a CFG grammar to generate the language. [6]
 i) $L = \{a^{2n} b^n \mid n > 0\}$
 ii) Palindrome strings of a's and b's.
- b) Convert the given grammar CFG to GNF. [6]
 $S \rightarrow ABA \mid AB \mid BA \mid AA \mid A \mid B$
 $A \rightarrow aA \mid a, B \rightarrow bB \mid b$
- c) Define ambiguous grammar. Is the following grammar ambiguous? [4]
 $S \rightarrow aAS \mid a, A \rightarrow SbA \mid SS \mid ba$

SECTION - II

- Q7)** a) Prove that $L = \{a^n b^n \mid n \geq 1\}$ is not regular using pumping lemma theorem. [6]
- b) State and Explain closure properties of regular expression with example. [6]
- c) Let $G = (\{A_0, A_1\}, \{a, b\}, P, A_0)$ [6]
 Where $P = \{A_0 \rightarrow A_1a, A_1 \rightarrow A_1b, A_1 \rightarrow a, A_1 \rightarrow A_0b\}$
 Convert given grammar Left linear grammar to equivalent Right linear grammar.

OR

- Q8)** a) Explain Chomsky hierarchy with an example. [6]
- b) Let $G = (\{S, B, A, C\}, \{0, 1\}, P, S)$ where [6]
 $P = \{S \rightarrow B1 \mid A0 \mid C0$
 $B \rightarrow B1 \mid 1$
 $A \rightarrow A1 \mid B1 \mid C0 \mid 0$
 $C \rightarrow A0$
 $\}$
 Construct a FA equivalent to given grammar.
- c) Construct a regular grammar G generating the regular set represented by
 $P = 0^* 1 (0 + 1)^*$ [6]

- Q9)** a) Construct PDA which accepts the language generated by the following CFG for arithmetic operations $S \rightarrow S+S \mid S*S \mid 4$ [8]
 b) Define post machines. Compare PDA and post machine. [4]
 c) Write a short note on closure properties of CFLs. [4]

OR

- Q10)** a) Construct equivalent CFG for given PDA. [8]

$$M = (\{q_0, q_1\}, \{0, 1\}, \{z_0, x\}, \delta, q_0, z_0, \Phi)$$

$$\delta(q_0, 1, z_0) = (q_0, xz_0)$$

$$\delta(q_0, 1, x) = (q_0, xx)$$

$$\delta(q_0, 0, x) = (q_1, x)$$

$$\delta(q_0, \wedge, z_0) = (q_0, \wedge)$$

$$\delta(q_1, 1, x) = (q_1, \wedge)$$

$$\delta(q_1, 0, z_0) = (q_0, z_0)$$

- b) Design PDA to accept the language $L = \{a^n b^{2n} \mid n > 1\}$ by a final state. [8]

- Q11)** a) Write short notes on: [8]

- i) Nondeterministic Turing Machine.
- ii) Halting Problem of Turing Machine.

- b) Design a Turing machine to compute 2's complement of given binary number. [8]

OROR

- Q12)** a) Design a Turing machine to add two unary numbers. [8]

- b) Write short notes on: [8]
- i) Limitations of TM.
 - ii) Universal Turing Machine.

