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DECEMBER 2017 / ENDSEM**F. Y. B. TECH. (COMMON) (SEMESTER - I)****Engineering Mathematics-I (ES11171)****(2017 PATTERN) (SET-A)**

Time: [2 Hours]

[Max. Marks: 50]

Instructions to candidates:

- 1) Q.1 is compulsory.
- 1) Answer Q.2 OR Q.3, Q.4 OR Q.5
- 2) Figures to the right indicate full marks.
- 3) Use of scientific calculator is allowed
- 4) Use suitable data where ever required.

Q.1) a) Find the rank of matrix $\begin{bmatrix} 1 & 3 & 6 \\ 1 & 4 & 5 \\ 1 & 5 & 4 \end{bmatrix}$. [2]

b) Find eigen values of the matrix $\begin{bmatrix} 14 & -10 \\ 5 & 1 \end{bmatrix}$. [2]

c) Find modulus & argument of complex number $\sqrt{\frac{1+i}{1-i}}$ [2]

d) Using Demoivre's theorem, find the value of $(1+i)^8 + (1-i)^8$. [2]

e) $y = 2\sin x \cos x$, then find y_n . [2]

f) If $y = \frac{1}{(x+1)^3}$, then find y_n . [2]

g) Express given complex no. in polar form $(-1+i)$. [2]

h) Under what condition, Raabe's test is applied? Also state Raabe's test. [2]

i) Write the Series expansion for $f(x) = e^{-x}$. [2]

j) Write the Series expansion for $f(x) = \cosh x$. [2]

P.T.O.

Q 2) a) Find the value of n for which $z = t^n e^{-r^2/4t}$ satisfies the partial differential

equation $\frac{1}{r^2} \left[\frac{\partial}{\partial r} \left(r^2 \frac{\partial z}{\partial r} \right) \right] = \frac{\partial z}{\partial t}$. [6]

b) If $u = \operatorname{cosec}^{-1} \sqrt{\frac{x^{1/2} + y^{1/2}}{x^{1/3} + y^{1/3}}}$, show that $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} = \frac{\tan u}{12} \left(\frac{13}{12} + \frac{\tan^2 u}{12} \right)$. [6]

c) If $u = f(x-y, y-z, z-x)$ then prove that $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = 0$. [4]

OR

Q3) a) If $u = \log(x^3 + y^3 + z^3 - 3xyz)$, prove that $\left(\frac{\partial}{\partial x} + \frac{\partial}{\partial y} + \frac{\partial}{\partial z} \right)^2 u = \frac{-9}{(x+y+z)^2}$. [6]

b) If $u = \sin^{-1}(x^3 + y^3)^{2/5}$, show that $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} = \frac{6}{5} \tan u \left(\frac{6}{5} \sec^2 u - 1 \right)$. [6]

c) If $ux + vy = 0$, $\frac{u}{x} + \frac{v}{y} = 1$, prove that $\left(\frac{\partial u}{\partial x} \right)_y - \left(\frac{\partial v}{\partial y} \right)_x = \frac{x^2 + y^2}{y^2 - x^2}$. [4]

Q4) a) If $x = u + v + w$, $z = u^3 + v^3 + w^3$, $y = u^2 + v^2 + w^2$, then show that $\frac{\partial u}{\partial x} = \frac{vw}{(u-v)(u-w)}$. [6]

b) The focal length of a mirror is found from $\frac{2}{f} = \frac{1}{v} - \frac{1}{u}$. Find the percentage error in f if u and v is both of error 2% each. [4]

c) Divide 120 into three parts such that the sum of their products taken two at a time shall be maximum. [4]

OR

Q5) a) Find the extreme values of $xy(a-x-y)$. [6]

b) Examine for the functionally dependent for $u = \sin^{-1} x + \sin^{-1} y$, $v = x\sqrt{1-y^2} + y\sqrt{1-x^2}$. Also find the relation between them if it exists. [4]

c) If the kinetic energy is $T = \frac{mV^2}{2}$. Find the approximate change in T as m changes from 49 to 49.5 and V changes from 1600 to 1590. [4]

-----ALL THE BEST-----