

G.R. No.

Paper Code - U127-101 (RE-F & FS)

JUNE 2018/1 RE-EXAM

F. Y. B. TECH. (COMMON) (SEMESTER - II)

COURSE NAME: Engineering Mathematics II

COURSE CODE: ES12171

(2017 PATTERN)

Time: [2 Hours]

[Max. Marks: 50]

(*) Instructions to candidates:

- 1) Answer Q.1 OR Q.2, Q.3 OR Q.4 and Q.5
- 2) Figures to the right indicate full marks.
- 3) Use of scientific calculator is allowed
- 4) Use suitable data wherever required

- Q.1) a) Find the equation of sphere on the join of the points (2,-3,1); (1,-2,-1) as its diameter. 6
- b) Obtain the equation of the right circular cone, which passes through the point (2, 1,3) with vertex is at (1,1,2) and axis parallel to the line $\frac{x-2}{2} = \frac{y-1}{-4} = \frac{z+2}{3}$. 6
- c) Find the equation of right circular cylinder whose guiding curve is $x^2 + y^2 + z^2 = 9, x - y + z = 3$ 4

OR

- Q.2) a) Find the equation of circle which is section to the sphere $x^2 + y^2 + z^2 + 6y - 6z - 21 = 0$ and having center at (2,-1,3). 6
- b) Obtain the equation of the right circular cone, with vertex is at (1,-1,2) and axis parallel to the line $\frac{x-1}{2} = \frac{y+1}{1} = \frac{z-2}{-2}$ and semi vertical angle 45° 6
- c) Find the equation of right circular cylinder whose axis is the line $\frac{x-2}{2} = \frac{y-3}{1} = \frac{z+1}{1}$ and radius is 5. 4

- Q.3) a) Express the following integral $\int_0^4 \int_{y/4}^1 e^{x^2} dx dy$ 6
- b) Evaluate $\int_0^1 \int_0^{\sqrt{1-x^2}} \int_0^{\sqrt{1-x^2-y^2}} \frac{dz dx dy}{\sqrt{1-x^2-y^2-z^2}}$ 4
- c) Find the total area of astroide $x^{2/3} + y^{2/3} = a^{2/3}$ 4

OR

- Q.4) a) Evaluate $\int_0^1 dx \int_1^\infty e^{-y} y^x \log y dy$ 6

b) Evaluate $\int_0^1 dx \int_0^{\sqrt{1-x^2}} e^{x^2+y^2} dy$ 4

c) Find the volume cut off by $x^2 + y^2 = z^2$ from sphere $x^2 + y^2 + z^2 = a^2$ 4

Q.5) Attempt following questions:[20 marks] 20

1 Find order and degree of the differential equation $\left(\frac{d^3y}{dx^3}\right)^2 + \left(\frac{dy}{dx}\right)^4 + y = 0$. 2

2 Find I.F. of the D.E. $\frac{dy}{dx} + 2xy = x^2$. 2

3 Find orthogonal trajectory for the family of $y = mx$ 2

4 What is amplitude of the first harmonic of Fourier series 2

5 Using DUIS rule find $\frac{d}{dx} \left(\int_x^{x^2} e^{-t^2} dt \right)$ 2

6 If $f(x) = a^2 - x^2$ in $0 < x < a$ then find value of a_0 in Fourier series 2

7 Evaluate $\int_0^\infty e^{-x} \sqrt{x} dx$. 2

8 Evaluate $I = \int_0^{2\pi} \sin^4 x dx$ 2

9 Find asymptotes of the curve $y^2(x-a) = x^2(2a-x)$. 2

10 Evaluate $\int_0^{\pi/2} \sqrt{\tan x} dx$. 2
