

Total No. of Questions :12]

SEAT No. :

P2466

[Total No. of Pages :4

[5153] - 100

T.E. (I.T.)

DESIGN AND ANALYSIS OF ALGORITHMS

(2008 Course) (Semester - II) (314455)

Time : 3 Hours]

[Max. Marks :100

Instructions to the candidates:

- 1) *Draw neat diagrams wherever necessary.*
- 2) *Assume suitable data if necessary.*
- 3) *Figures to the right indicate full marks.*

SECTION -I

Q1) a) Find out the time complexity for the recurrence equation as follows: **[8]**

i) $T(n) = T(n/2) + 1$

ii) $T(n) = 2T(n/2) + n$

Also explain whether above equations belong to Searching or Sorting.

b) Prove by contradiction - “there are infinitely many prime numbers”. **[8]**

OR

Q2) a) Suppose you have algorithms with running time listed below. How much faster will they get if input size is reduced by half. **[8]**

i) $100n^2$

ii) $n \log n$

iii) 2^n

iv) n^2

b) Write an algorithm to search an element in an array of size n. Calculate complexity of this algorithm. **[8]**

P.T.O.

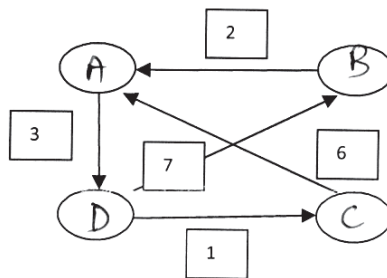
- Q3)** a) What is divide and conquer strategy? Explain Master's theorem. [8]
b) Explain convex hull problem with a suitable example. [8]

OR

- Q4)** a) Which algorithm uses the principle of decrease-by-half? Why is it called so? [8]
b) Write Kruskal's algorithm. Comment on its complexity. [8]
- Q5)** a) What is memory function? Explain why it is advantageous to use memory functions. [9]
b) Explain with suitable example Warshall's algorithm. [9]

OR

- Q6)** Find all-pairs shortest path using Floyd's algorithm for the following weighted graph. [18]



SECTION -II

- Q7)** a) Explain the following terms: [8]
Live nodes, expanding nodes, bounding function and solution space.
b) What are planar graphs? Explain graph coloring with suitable examples. [8]

OR

Q8) What is backtracking? What kind of problems does it solve? Solve the following knapsack problem using backtracking. **[16]**

i	p_i	w_i
1	24	15
2	15	10
3	25	18

For $n=3$ and $m=20$.

Q9) a) Explain the terms: **[9]**

Branch and Bound, LC, LIFO and Bounding function. How are LIFO and LC techniques different?

b) Differentiate between Backtracking and Branch and Bound. **[9]**

OR

Q10) Solve the following job scheduling problem using LCBB. **[18]**

Job	p_i	d_i	t_i
1	5	1	1
2	10	3	2
3	6	2	1
4	3	1	1

Where P_i : indicates penalty if i^{th} job is not completed by deadline d_i . p_i has burst time t_i . We want to have minimum penalty.

- Q11)**a) What is a deterministic and non-deterministic algorithm? Write a non-deterministic algorithm for searching an element. [8]
- b) Prove that: A clique problem is NP-complete. [8]

OR

- Q12)**a) What is satisfiability problem? Explain DNF and CNF. [8]
- b) Explain NP-Complete and NP-Hard. Give examples. Are all NP-Complete problems NP-Hard or vice versa? Justify. [8]

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