

[5254]-24

B.E. (Civil Engineering) (Semester - II)

FINITE ELEMENT METHOD IN CIVIL ENGINEERING

(2008 Pattern) (Open Elective)

Time : 3 Hours]

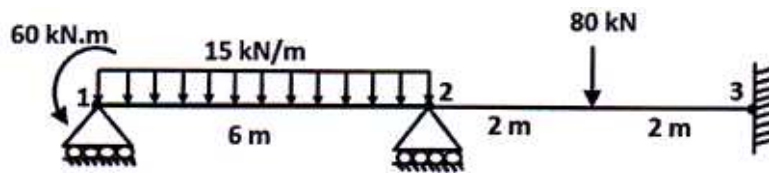
[Max. Marks : 100

*Instructions to the candidates:*

- 1) Answer to the two sections should be written in separate books.
- 2) Figures to the right indicate full marks.
- 3) Neat diagrams must be drawn wherever necessary.
- 4) Use of non programmable calculator is allowed.
- 5) Assume suitable data, if necessary.

**SECTION - I**

**Q1)** Determine the rotations of nodes 1 and 2 and bending moments for the beam as shown in figure using finite element method. Take  $EI = 20 \times 10^3 \text{ kN.m}^2$  [18]



OR

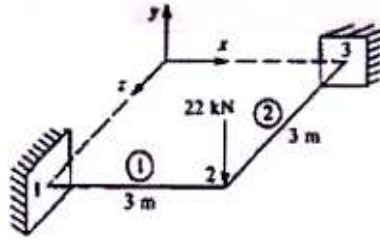
- Q2)** a) Derive  $4 \times 4$  stiffness matrix for the truss member using finite element formulation. [12]
- b) Explain step by step procedure of FEM. [6]

**Q3)** Derive the stiffness matrix of two noded frame element with six degrees of freedom. Derive the transformation matrix for the two noded frame element. [16]

OR

**P.T.O.**

- Q4)** The grid consists of two elements fixed at nodes 1 and 3. Find displacement and rotations at node 2. Take  $E = 210\text{GPa}$ ;  $G = 84\text{GPa}$ ;  $I = 16.6 \times 10^{-5} \text{ m}^4$  and  $J = 4.6 \times 10^{-5} \text{ m}^4$ . [16]



- Q5)** a) Explain in brief state of stress and strain at a point. [8]  
 b) Derive the differential equations of equilibrium in case of three-dimensional stress system. [8]

OR

- Q6)** a) Explain plane stress and plane strain elasticity problem with example. Write stress-strain relationship. [8]  
 b) Derive stress compatibility condition for 2D plane stress elasticity problem. [8]

### SECTION - II

- Q7)** a) Give two dimensional and three dimensional Pascal's triangle. Explain its use in FEM analysis. [9]  
 b) What is aspect ratio of element? How it affect the FEM solution? Explain with suitable example. [9]

OR

- Q8)** a) State and explain the convergence criteria for the choice of the displacement function in FEM with examples. [9]  
 b) Enlist the various 1D, 2D and 3D elements with diagrams used in finite element analysis. [9]

- Q9)** a) What are Serendipity elements explain with examples? Derive shape functions of four noded serendipity element. [8]  
 b) Obtain strain displacement matrix for a CST element. [8]

OR

- Q10)**a) Derive shape functions for the nine noded rectangular elements in natural coordinate ( $\xi, \eta$ ) system using Lagrange's interpolation function. [8]
- b) Derive the relationship between the natural (area) and Cartesian coordinates of a triangular element. [8]

- Q11)**a) Explain Jacobian matrix in case of four noded isoperimetric quadrilateral element. Obtain strain displacement matrix. [12]
- b) State and explain three basic laws on which isoparametric concept is developed. [4]

OR

- Q12)** Explain strain-displacement and stress-strain relationships for 3D problem. Hence, derive necessary matrices for formulation of stiffness matrix of 3D tetrahedron element. [16]

