

Total No. of Questions : 8]

SEAT No. :

P4013

[5255]-510

[Total No. of Pages : 2

M.E. (Civil - Structures)

ADVANCED MECHANICS OF SOLIDS

(2013 Pattern) (Credit Course)

Time : 3 Hours]

[Max. Marks : 50

Instructions to the candidates:

- 1) *Attempt any five questions from the following.*
- 2) *Neat diagrams must be drawn wherever necessary.*
- 3) *Figures to the right indicate full marks.*
- 4) *Assume suitable data, if necessary and clearly state.*
- 5) *Use of cell phone is prohibited in the examination hall.*
- 6) *Use of electronic pocket calculator is allowed.*

Q1) a) Obtain Strain compatibility Equation for 2D problem in Elasticity. **[5]**

b) Explain concept of stress at a point and stress on inclined plane. **[5]**

Q2) a) Define Airys stress function. Prove that stress function ϕ satisfying the governing equation $\nabla^4 \phi = 0$, when body force is absent. **[6]**

b) State and explain generalised Hooks law. Express the stress strain relation for an elastic and isotropic body in terms of engineering constant E and ν . **[4]**

Q3) a) Derive differential equation of equilibrium of plane elasticity problem in polar co-ordinate with usual notation. **[7]**

b) What is axisymmetric problem. Show that for such a problem, the stress function $\phi = A \log r + B r^2 \log r + C r^2 + D$. **[3]**

Q4) a) Derive an expression for radial (σ_r) and tangential (σ_t) stresses for thick cylinder of internal radius (r_i) and external radius (r_o) subjected to internal pressure (p_i) **[6]**

b) Derive component of stress due to circular hole in a stressed plate (Michell's problem). **[4]**

P.T.O.

Q5) A quarter circle beam of radius 1 m curved in plan is fixed at A and free at B. It carries vertical downward load $P = 25$ kN at free end B. Determine maximum bending moment, torsional moment and deflection. Also draw shear force, bending moment and torsional moment diagram. **[10]**

Q6) a) Show that the neutral axis of curve beam in elevation is below the centroidal axis towards the center of curvature. **[6]**

b) Differentiate between beam curve in plan and elevation. **[4]**

Q7) Assuming $\phi = m(x^2 / a^2 + y^2 / b^2 - 1)$ as a stress function for a bar of elliptical cross section subjected to pure torque M_t about its longitudinal axis, find moment and shear stress components. **[10]**

Q8) a) Derive differential equation for a beam resting on elastic foundation. **[4]**

b) An infinitely long steel beam of unit width and 250 mm thick is resting on elastic foundation whose modulus of foundation is 10 N/mm^2 . A concentrated load of 12 kN is applied at a point. Determine maximum deflection and maximum bending stress assuming $E = 200 \text{ GPa}$. **[6]**

