

Total No. of Questions :8]

SEAT No. :

P4017

[Total No. of Pages :2

[5255] - 514

M.E. (Civil - Structural Engineering)

FINITE ELEMENT ANALYSIS

(2013 Pattern) (Semester - II)

Time : 3 Hours]

[Max. Marks :50

Instructions to the candidates:

- 1) *Attempt any five questions.*
- 2) *Neat diagrams must be drawn wherever necessary.*
- 3) *Figures to the right indicate full marks.*
- 4) *Use of non programmable electronic calculator is allowed.*
- 5) *Assume suitable data, if necessary.*

Q1) a) For the following boundary value problem solve using point collocation

method $\frac{d^2u}{dx^2} - u = x$ $0 \leq x \leq 1$. The conditions given are $u(0) = 0$ and $u(1) = 0$. Choose $x = 0.25$ and 0.5 as the collocation points. Consider the approximate solution in form of $a_1(x - x^2) + a_2(x^2 - x^3)$. **[6]**

b) Derive elemental stiffness matrix for a plane truss element or 1 - D bar element using variational approach. **[4]**

Q2) a) From the fundamentals derive the shape functions of CST element in area coordinates and hence obtain strain - displacement matrix for the element. **[5]**

b) Explain the use of Pascal's triangle in formulation of displacement function in Finite element method. Explain with suitable examples, compatible and completeness requirements of displacement functions. **[5]**

Q3) Analyse the plane truss shown in the Fig. 1 using direct method of finite element method. Take $AB=1000$ mm, $BC=1000$ mm and height of truss = 1000 mm. D point is at center of CB and subjected to horizontal load of 200 kN. Young's Modulus is 200 GPa **[10]**

P.T.O.

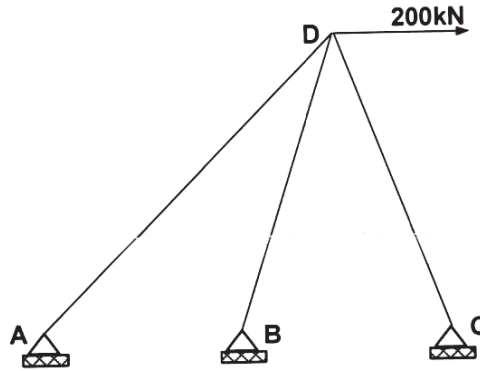


Fig. 1

- Q4)** a) What are serendipity elements? Derive the shape function for eight noded serendipity element in Cartesian or natural coordinate system. [6]
- b) For a tetrahedral element derive the shape function in terms of the volume of tetrahedral and express the displacements in terms of shape function. [4]
- Q5)** a) Write the expressions for normal and shear strain for the axisymmetric element and give the isotropic stress/strain relationship for the axisymmetric element. [3]
- b) Derive the stiffness matrix for a typical triangular axisymmetric element starting from fundamentals. [7]
- Q6)** Explain the term Jacobian matrix. Formulate strain displacement matrix for a two dimensional isoparametric element in plane elasticity problem, using Jacobian matrix. [10]
- Q7)** Write a short note on any one type of plate bending elements. Explain conformity of the displacement function of the element. [10]
- Q8)** a) Which elements are called as shell elements? Write short note on Flat shell element. [5]
- b) Write a note on Ahmad's degenerated solid element. [5]

