Seat No.

[5252]-171

S.E. (Infor. Tech.) (First Semester) EXAMINATION, 2017 DISCRETE STRUCTURE (2012 COURSE)

Time: Two Hours

Maximum Marks: 50

- N.B.: (i) Answer Q. No. 1 or Q. No. 2, Q. No. 3 or Q. No. 4, Q. No. 5 or Q. No. 6, Q. No. 7 or Q. No. 8.
 - (ii) Draw neat diagrams must be drawn wherever necessary.
 - (iii) Figures to the right indicate full marks.
 - (iv) Assume suitable data, if necessary.
- 1. (a) What are different logical connections? Define all logical connections with the help of proper example. [6]

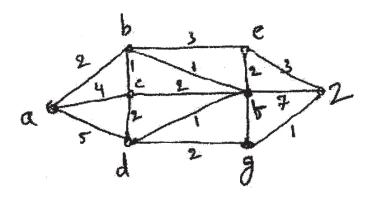
(b) P.T.
$$\frac{1}{4} + \frac{1}{4.7} + \frac{1}{7.10} + \dots + \frac{1}{(3n-2)(3n+1)} = \frac{n}{3n+1}$$
 [6]

- 2. (a) A survey of 70 high school students revealed that 35 like folk music, 15 like classical music, and 5 like both. How many of the students surveyed do not like either folk or classical music?
 - (b) What is an equivalent relation? Identify whether the given relation is an equivalent relation where

 A = {1, 2, 3, 4}, R = {(1, 1), (1, 2), (2, 1), (2, 2), (3, 1), (3, 3), (1, 3), (4, 1) (4, 4,). Also find the equivalent classes.

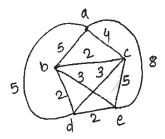
 [6]

- **3.** (a) What is monoid? Show that the algebraic system (A, +) is a monoid, where A is set of integers and + is a binary operation giving addition of two integers. [6]
 - (b) Find the shortest path from a to z, using Dijkstra's Algorithm. [6]



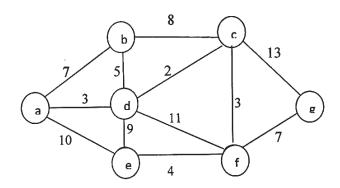
Or

- 4. (a) Show that the graph G and G^* are isomorphic G = (V, E) and $G^* = (V^*, E^*)$ given by : [6] $G = (\{a, b, c, d\}, \{(a, b), (a, d), (b, d), (c, d), (c, b), (b, c)\}).$
 - $G^* = (\{(1,\ 2,\ 3,\ 4\},\ \{(1,\ 2),\ (2,\ 3),\ (3,\ 1),\ (3,\ 4),\ (4,\ 3),\\ (4,\ 2)\}).$
 - (b) (i) Define Graph Coloring. [2]
 - (ii) User nearest neighbor method to find Hamiltonian circuit starting from a, find its weight. [4]



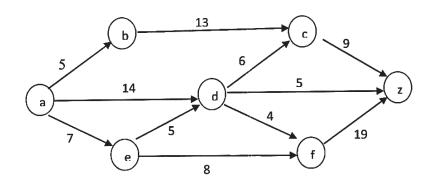
5. (a) For the following set of weight, construct the optimal binary prefix tree. For each of the weight in the set, give the corresponding prefix code. [6]

(b) Determine the minimum spanning tree using prims algorithm for the following graph: [6]



Or

6. (a) A find maximum flow in the following transport network. [6]



- (b) Represent the following expression as: [6]
 - (1) A binary tree
 - (2) Postfix Notation
 - (3) Prefix Notation.

$$((a + b)*c)/((d - e) ^f)$$

- 7. (a) How many auto license number plates can be created with 3 alphabets followed by 4 digits if: [4]
 - (1) Repetition of both alphabets and numbers is allowed.
 - (2) Repetition of both alphabets and number is not allowed.
 - (b) In how many ways can five examinations be scheduled in a week so that no two examinations scheduled on same day considering Sunday as holiday? [3]
 - (c) A committee of 5 members is to be formed from a group of 7 men and 6 women. What is the probability that:
 - (1) At least 3 women are part of the committee.
 - (2) All committee members are either men or women. [6] Or
- 8. (a) Out of 15 employees in a software company, a group of 5 employees is to be sent for for 'Linux Administration and Networking' training of one month. [7]
 - (1) In how many ways can the 5 employees be selected?
 - (2) What if there are 2 employees who refuse to go together for training ?
 - (3) What if there are 2 employees who want to go together i.e. either they go together or they do not go for training?
 - (b) Two cards are drawn at random from an ordinary deck of well shuffled 52 cards. Find the probability that : [6]
 - (1) First cards drawn is ace and second cards drawn is face card of spade.
 - (2) Both are spades.