

[5353]-196

T.E. (Information Technology)

DESIGN AND ANALYSIS OF ALGORITHMS

(2012 Pattern)

Time : 2½ Hours]

[Max. Marks : 70

Instructions to the candidates:

- 1) Answer Q1 or Q2, Q3 or Q4, Q5 or Q6, Q7 or Q8, Q9 or Q10.
- 2) Neat diagram must be drawn whenever necessary.
- 3) Figures to the right side indicate full marks.
- 4) Assume Suitable data if necessary.

**Q1)** a) Explain direct proof & proof by counter example techniques. [4]

b) Define following asymptotic notations : [6]

- i) Theta
- ii) Little oh
- iii) Little Omega

OR

**Q2)** a) Setup a recurrence relation to compute  $n!$  and solve it. [5]

b) Consider the following letters with their probability. [5]

Character	a	b	c	d	e
Probability	0.5	0.25	0.125	0.625	0.031

Find out Huffman coding for a, b, c, d, e.

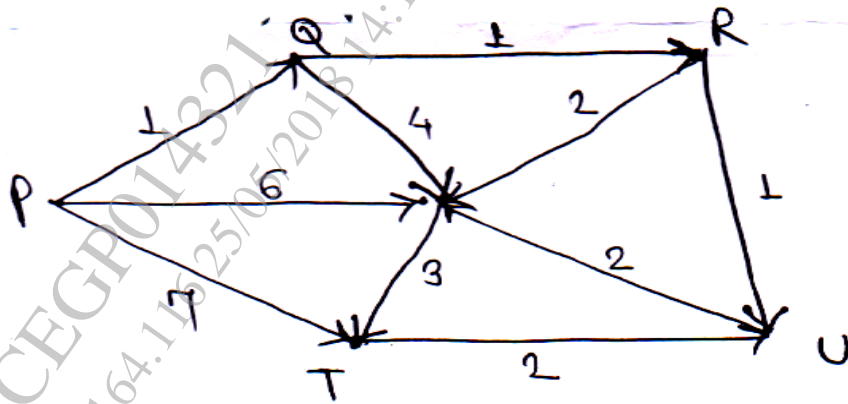
**Q3)** a) Show the steps in multiplying the following two integers using efficiency integer multiplication method  $2101 \times 1130$ . [5]

b) Explain the following terms with reference to Greedy Technique [5]

- i) Feasible solution and optimal solution
- ii) Subset paradigm and ordering paradigm

OR

- Q4) a)** Apply Dijkstra's algorithm for finding all shortest paths from a single source 'p' in a given graph [5]



- b) Explain the concept of divide and conquer technique. Write master theorem. [5]

- Q5) a)** Let  $w = \{5, 10, 12, 13, 15, 18\}$ ,  $m = 30$ . Find all possible subsets of  $w$  that sum to  $m$ . Draw the portion of state space tree that is generated. [8]
- b) Write a recursive backtracking algorithm for  $m$ -coloring of the graph. [8]

OR

- Q6) a)** What is  $m$ -colorability optimization problem? Explain with an example. [8]
- b) Find all possible solutions for 5 queens' problem using backtracking method. [8]

- Q7)** What is travelling salesman problem? Find the solution of following travelling salesman problem using branch and bound method. [18]

$\infty$	20	30	10	11
15	$\infty$	16	4	2
3	5	$\infty$	2	4
19	6	18	$\infty$	3
16	4	7	16	$\infty$

Cost Matrix

OR

- Q8)** a) What is LC Search? Explain in detail control abstraction for LC search. [8]  
b) Solve the following instance of 0/1 knapsack problem by FIFO branch and bound approach.  $n = 4$ ,  $M = 15$  and  $(P_1, P_2, P_3, P_4) = (10, 10, 12, 18)$ ;  $(W_1, W_2, W_3, W_4) = (2, 4, 6, 9)$  [10]
- Q9)** a) What do you mean by P, NP, NP-Hard and NP-complete problems? Give an example of each category. [8]  
b) Explain the need and significance of parallel algorithms. [8]

OR

- Q10)** a) Explain the following : [8]  
i) Computational complexity  
ii) Decision problems  
iii) Deterministic and Non - deterministic classes  
iv) Complexity classes  
b) Explain the possible parallel computations using complete binary tree. [8]

