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U218-151 (ESE)

DECEMBER 2018/ENDSEM

S. Y. B. TECH. (MECHANICAL ENGINEERING) (SEMESTER - I)

COURSE NAME: Engineering Mathematics III

COURSE CODE: MEUA21171

(PATTERN 2017)

Time: [2 Hours]

[Max. Marks: 50]

Instructions to candidates:

- 1) Answer Q.1, Q.2, Q.3, Q.4, Q.5 OR Q.6, Q.7 OR Q.8
- 2) Figures to the right indicate full marks.
- 3) Use of scientific calculator is allowed
- 4) Use suitable data where ever required

Q.1) a) $(D^2 + 9)y = x^3 + 2x - \cos 3x$ [6 marks]

OR

b) $x^3 \frac{d^2 y}{dx^2} + 3x^2 \frac{d^2 y}{dx^2} + xy = \sin(\log x)$ [6 marks]

Q.2) a) Using Fourier integral representation, show that

$$\int_0^{\infty} \frac{\lambda^3 \sin \lambda x}{\lambda^4 + 4} d\lambda = \frac{\pi}{2} e^{-x} \cos x, \text{ where } x > 0 \text{ [6 marks]}$$

OR

b) Find inverse Laplace transform of $\frac{s}{s^4 + 1}$ [6 marks]

Q.3) a) The first four moments of a distribution about the value 5 are 2, 20, 40 and 50. Calculate the first four central moments, mean, standard deviation, coefficient of skewness and kurtosis [6 marks]

OR

b) In a normal distribution 7% of the items are under 35 and 89% are under 63. Find the mean and standard deviation.

(Given: For $z=1.475$ area $A=0.43$, $z=1.226$ area $A=0.39$). [6 marks]

Q.4) a) Show that $\vec{F} = (6xy + z^3)\vec{i} + (3x^2 - z)\vec{j} + (3xz^2 - y)\vec{k}$ is irrotational.

Find scalar ϕ such that $\vec{F} = \nabla\phi$

[4 marks]

OR

b) $\nabla^2(\phi\phi) = \phi\nabla^2\phi + 2\nabla\phi \cdot \nabla\phi + \phi\nabla^2\phi$

[4 marks]

Q. 5 a) Find the work done in moving a particle from (1,1,1) to (3, -5, 7) in a force field

$\vec{F} = (x^2 - yz)\vec{i} + (y^2 - zx)\vec{j} + (z^2 - xy)\vec{k}$ [6 marks]

b) Using Stoke's Theorem evaluate following line integrals $\int_C (4y dx + 2z dy + 6y dz)$ where C is curve of intersection of $x^2 + y^2 + z^2 = 2z$ and $x = z - 1$.

[4 marks]

c) Show that $\iiint_V \frac{dV}{r^2} = \iint_S \left(\frac{\vec{r}}{r^2}\right) \cdot \hat{n} dS$ [4 marks]

OR

Q.6) a)) Verify Green's Theorem for

$\vec{F} = x\vec{i} + y^2\vec{j}$ over the first quadrant of the circle $x^2 + y^2 = a^2$.

[6 marks]

b) Using Stoke's Theorem evaluate following line integrals:

$\int_C (y dx + z dy + x dz)$ where C is the curve of intersection of $x^2 + y^2 + z^2 = a^2$ and $x + z = a$. [4 marks]

c) Evaluate $\iint_S (y^2z^2\vec{i} + z^2x^2\vec{j} + x^2y^2\vec{k}) \cdot d\vec{S}$ where S is surface of the sphere $x^2 + y^2 + z^2 = a^2$ in the positive octant. [4 marks]

Q.7) a) Solve $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$ if i) u is finite for all t , ii) u = 0 when x = 0, π for all t iii)

$u = \pi x - x^2$ when t = 0 and $0 \leq x < \pi$ [6 marks]

b) A rectangular plate with insulated surface is 10cm wide and so long compared to its width that it may be considered infinite in length without introducing an appreciable error . If the temperature along short edge y=0 is given

$u(x,0) = 100\sin\frac{\pi x}{10}, 0 \leq x \leq 10$, while the two long edges x = 0 and x = 10 as well as the other

short edge are kept at 0° C . State the conditions in mathematical form. [4 marks]

c) In Q.7 b, Find steady-state temperature u(x,y). [4 marks]

OR

Q.8) a) A tightly stretched string with fixed end points x=0 and x=l is initially in a

position given by $y(x,0) = y_0 \sin^3 \frac{\pi x}{l}$. If it is released from rest from this position , find the

displacement y at any distance x from one end and at any time t .

[6marks]

b) A tightly stretched string with fixed end points $x=0$ and $x=l$ is initially in a position given by $y(x,0) = y_0 \sin^3 \frac{\pi x}{l}$. If it is released from rest from this position, state the condition in mathematical form.

[4 marks]

c) Find the displacement y in the above problem Q.8 b at any distance x from one end and at any time t .

[4 marks]
