

Q.1) a)

K-Map - 2 Mark

Logical Expression - 1 Mark

Logic Circuit Diagram - 3 Mark.

Q.1) b)

Step 1: Binary equivalent of group minterm table - 2 Marks.

Step 2: List of prime implicant table - 1 Mark.

Step 3: Table of matched and unmatched minterm + 1 Mark

Step 4: Essential Prime implicant table - 1 Mark.

Step 5: final terms representation - 1 Marks.

Q.2) c) i)

Binary conversion of integral part - 1 mark

Binary conversion of fractional part - 1 Mark.

Q.1) c) ii) Sum of powers of 2's term - 1 Mark.

Binary representation - 1 Mark.

Q.2) a) Step 1: Canonical SOP form - 1 Mark.

Step 2: K-Map - 2 Marks

Step 3: Logical Circuit Diagram - 2 Marks.

Step 4: Expression - 1 Mark.

Q.2) b) Step 1: find out minterm and Binary equivalent of group minterm table - 2 Marks.
Step 2 to Step 5 $\rightarrow$ same as Q.1 b).

Q.2) c) Step 1: find Binary equivalent of number - 2 Marks
Step 2: write 8 bit positive number and
2's complement, - 2 Marks.

Q.3) a) table conversion (BCD to Excess-3) - 2 Marks
K-map - 2 Marks.
Logic circuit diagram - 2 Marks.

Q.3) b) Cascading of tree structure - 3 Marks.
table - 1 Mark.

Q.3) c) table - 1 Mark
K-Map - 1 Mark
Expression - 1 Mark.
Circuit Diagram - 1 Mark.

Q.4) A) - standard SOP form expression - 3 Marks.
Multiplexer Structure - 3 Marks.

Q.4) B) Truth Table - 1 Mark.
~~3:8~~ Expression - 1 Mark.
3:8 Decoder Structure - 2 Mark.

Q.4) C) Truth table - 1 Mark.
K-map - 1 Mark.
Expression - 1 Mark.
Circuit Diagram - 1 Mark.

Solution & Model Answer.

U218-125(T1)

Total No. of Questions - [04]

Total No. of Printed Pages 02

G.R. No.	
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OCTOBER 2018/ IN-SEM (T1)

S. Y. B. TECH. (COMPUTER ENGINEERING) (SEMESTER - I)

COURSE NAME: DIGITAL SYSTEMS AND LOGIC DESIGN

COURSE CODE: CSUA21175

(PATTERN 2017)

Time: [1 Hour]

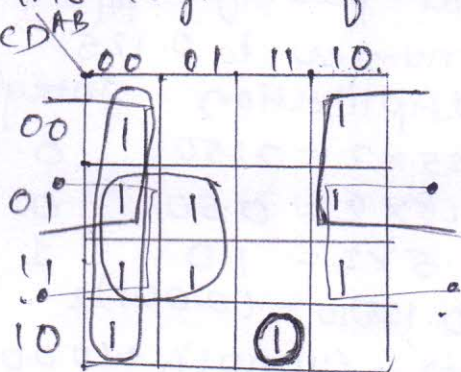
[Max. Marks: 30]

Instructions to candidates:

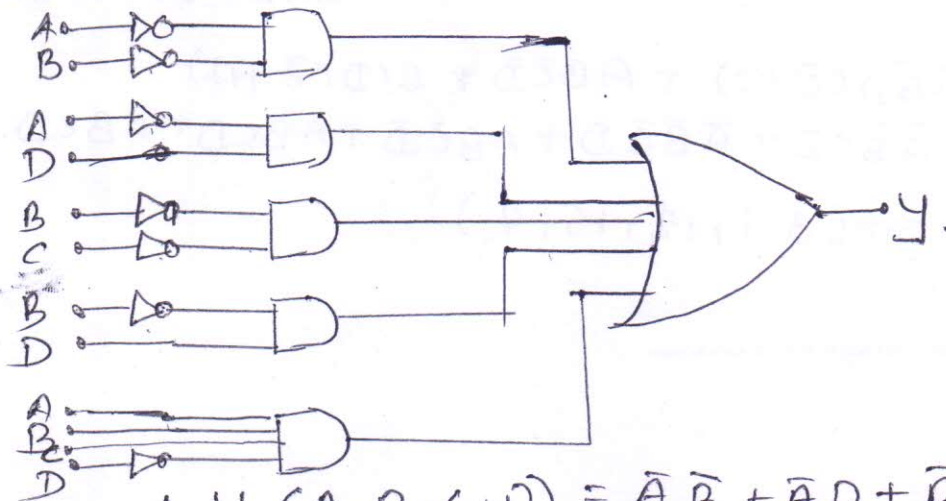
- 1) Answer Q.1 OR Q.2 and Q.3 OR Q.4.
- 2) Figures to the right indicate full marks.
- 3) Use of scientific calculator is allowed
- 4) Use suitable data wherever required

Q.1) a) $y(A, B, C, D) = \sum m(0, 1, 2, 3, 5, 7, 8, 9, 11, 14)$ [6M]

The logical function is $y(A, B, C, D) = \bar{A}\bar{B} + \bar{A}D + \bar{B}\bar{C} + \bar{B}D + ABC\bar{D}$.



$$y(A, B, C, D) = \bar{A}\bar{B} + \bar{A}D + \bar{B}\bar{C} + \bar{B}D + ABC\bar{D}$$



$$y(A, B, C, D) = \bar{A}\bar{B} + \bar{A}D + \bar{B}\bar{C} + \bar{B}D + ABC\bar{D}$$

Q.1b)

step 1:

Minterm	Binary	Minterm	Binary
m2	0010	m2	0010
m4	0100	m4	0100
m5	0101	m5	0101
m9	1001	m9	1001
m12	1100	m12	1100
m13	1101	m13	1101

Binary equivalents of groups of minterms.

step 3

Prime implicants	Binary
2	0010
9, 13	1-01
4, 5, 12, 13	-10-

step 2

minterms	Binary	minterms	Binary
4, 5	010- _L	4, 5, 12, 13	-10-
4, 12	-100 _L		
5, 13	-101 _L		
9, 13	1-01 _L		
12, 13	110- _L		

The list of prime implicant

step 4

Prime implicants	m2	m4	m5	m9	m12	m13
2		•				
9, 13				•		•
4, 5, 12, 13		•	•		•	•

$$\text{Step 5: } Y(A, B, C, D) = (1-01) + (-10-) \\ = A\bar{C}D + B\bar{C}$$

Q.1) $(109)_{10} = (1101101)_2$

	Quotient	Remainder
$109 \div 2$	54	1 LSB
$54 \div 2$	27	0
$27 \div 2$	13	1
$13 \div 2$	6	1
$6 \div 2$	3	0
$3 \div 2$	1	1
$1 \div 2$	0	1 MSB

(2) a)

* fractional part of the given number is 0.125.

Multiplication Integer part

$$0.125 \times 2 = 0.250 \quad 0 \text{ MSB}$$

$$0.25 \times 2 = 0.50 \quad 0$$

$$0.5 \times 2 = 1.0 \quad 1 \text{ LSB}$$

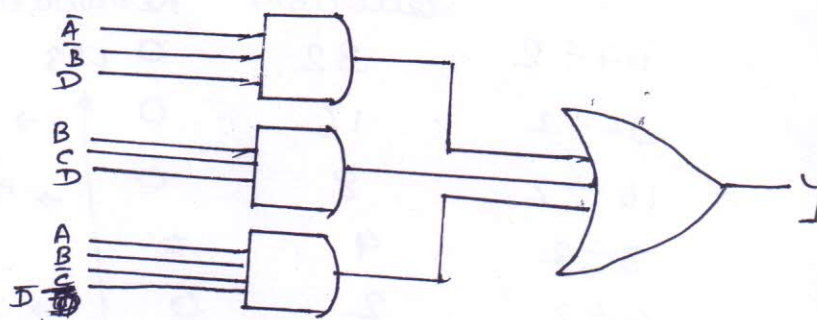
$$(0.125)_{10} = (0.001)_2$$

OR $(109.125)_{10} = (1101101)_2 + (0.001)_2 = (1101101.001)_2$

$$Y(A, B, C, D) = \bar{A}\bar{B}D(\bar{C}+C) + AB\bar{C}\bar{D} + BCD(\bar{A}+A) \\ = \bar{A}\bar{B}CD + \bar{A}\bar{B}\bar{C}\bar{D} + AB\bar{C}\bar{D} + ABCD + \bar{A}BCD$$

$$Y(A, B, C, D) = \sum m(3, 1, 12, 15, 7)$$

AB \ CD	00	01	11	10
00			1	
01	1			
11	1	1	1	
10				



$$Y(A, B, C, D) = \bar{A}\bar{B}D + BCD + AB\bar{C}\bar{D}$$

Q.2) b) $Y(A, B, C, D) = \Pi M(1, 4, 6, 9, 10, 11, 14, 15)$

[6]

$$Y(A, B, C, D) = \sum m(0, 2, 3, 5, 7, 8, 12, 13)$$

Minterms	Binary	Minterm	Binary
m_0	0000	m_0	0000L
m_2	0010	m_2	0010L
m_3	0011	m_8	1000L
m_5	0101	m_3	0011L
m_7	0111	m_2	1100L
m_8	1000	m_5	0101L
m_{12}	1100	m_7	0111L
m_{13}	1101	m_{13}	1101L

Minterm	Binary	Minterm	Binary
0, 2	00-0		
0, 8	-000		
2, 3	001-		
8, 12	1-00		
3, 7	0-11		
5, 7	01-1		
5, 13	-101		
12, 13	110-		

1. Minterms in binary equivalent & group of minterms.

2. Binary equivalent of group of minterms with check marks.

Prime Implicants	Binary
0, 2	00-0
0, 8	-000
2, 3	001-
8, 12	1-00
3, 7	0-11
5, 7	01-1
5, 13	-101
12, 13	110-

List of Prime Implicants

Prime Implicants	m_0	m_2	m_3	m_5	m_7	m_8	m_{12}	m_{13}
0, 2L	•	•						
0, 8L	•					•		
2, 3		•	•			•		
8, 12			•			•	•	
3, 7			•		•			
5, 7				•	•			
5, 13				•				•
12, 13							•	•

Prime Implicant selection

$$\neg(A \neg B \neg C D) = (\neg 110 \neg) + (\neg \neg 101) + (\neg 01 \neg) + (\neg \neg 000) + (\neg 00 \neg) \\ = AB\bar{C} + B\bar{C}D + \bar{A}CD + \bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{D} \quad (4)$$

Q.2) (64)₁₀ Quotient Remainder

$$64 \div 2 \quad 32 \quad 0 \text{ LSB}$$

$$32 \div 2 \quad 16 \quad 0$$

$$16 \div 2 \quad 8 \quad 0$$

$$8 \div 2 \quad 4 \quad 0$$

$$4 \div 2 \quad 2 \quad 0$$

$$2 \div 2 \quad 1 \quad 0$$

$$1 \div 2 \quad 0 \quad 1 \text{ MSB}$$

$$\rightarrow (64)_{10} = (1000000)_2$$

→ Positive number using 8-bits.

$$(+64)_{10} = (01000000)_2$$

→ 2's complement represents of the no. is same as the sign magnitude represent of positive numbers.

Q3) a)

Decimal Digit	BCD code				Excess-3 code			
	B ₃	B ₂	B ₁	B ₀	E ₃	E ₂	E ₁	E ₀
0	0	0	0	0	0	0	1	1
1	0	0	0	1	0	1	0	0
2	0	0	1	0	0	1	0	1
3	0	0	1	1	0	1	1	0
4	0	1	0	0	0	1	1	1
5	0	1	0	1	0	1	1	1
6	0	1	1	0	1	0	0	0
7	0	1	1	1	1	0	0	1
8	1	0	0	0	1	0	1	0
9	1	0	0	1	1	0	1	1

B ₃ B ₂	00	01	11	10
00	0	0	X	1
01	0	1	X	1
11	0	1	X	X
10	0	1	X	X

$$K\text{-map for } E_3 = B_3 + B_2B_0 + B_2B_1$$

B ₃ B ₂	00	01	11	10
00	0	1	X	0
01	1	0	X	1
11	1	0	X	X
10	1	0	X	X

$$E_2 = \bar{B}_2B_0 + \bar{B}_2B_1 + B_2\bar{B}_1\bar{B}_0$$

$B_3 B_2$ $B_1 B_0$	00	01	11	10
00	1	1	X	1
01	0	0	X	0
11	1	1	X	X
10	0	0	X	X

$$E_1 = \bar{B}_1 \bar{B}_0 + B_1 B_0$$

$B_3 B_2$ $B_1 B_0$	00	01	11	10
00	1	1	X	1
01	0	0	X	0
11	0	0	X	X
10	1	1	X	X

$$E_0 = \bar{B}_0$$

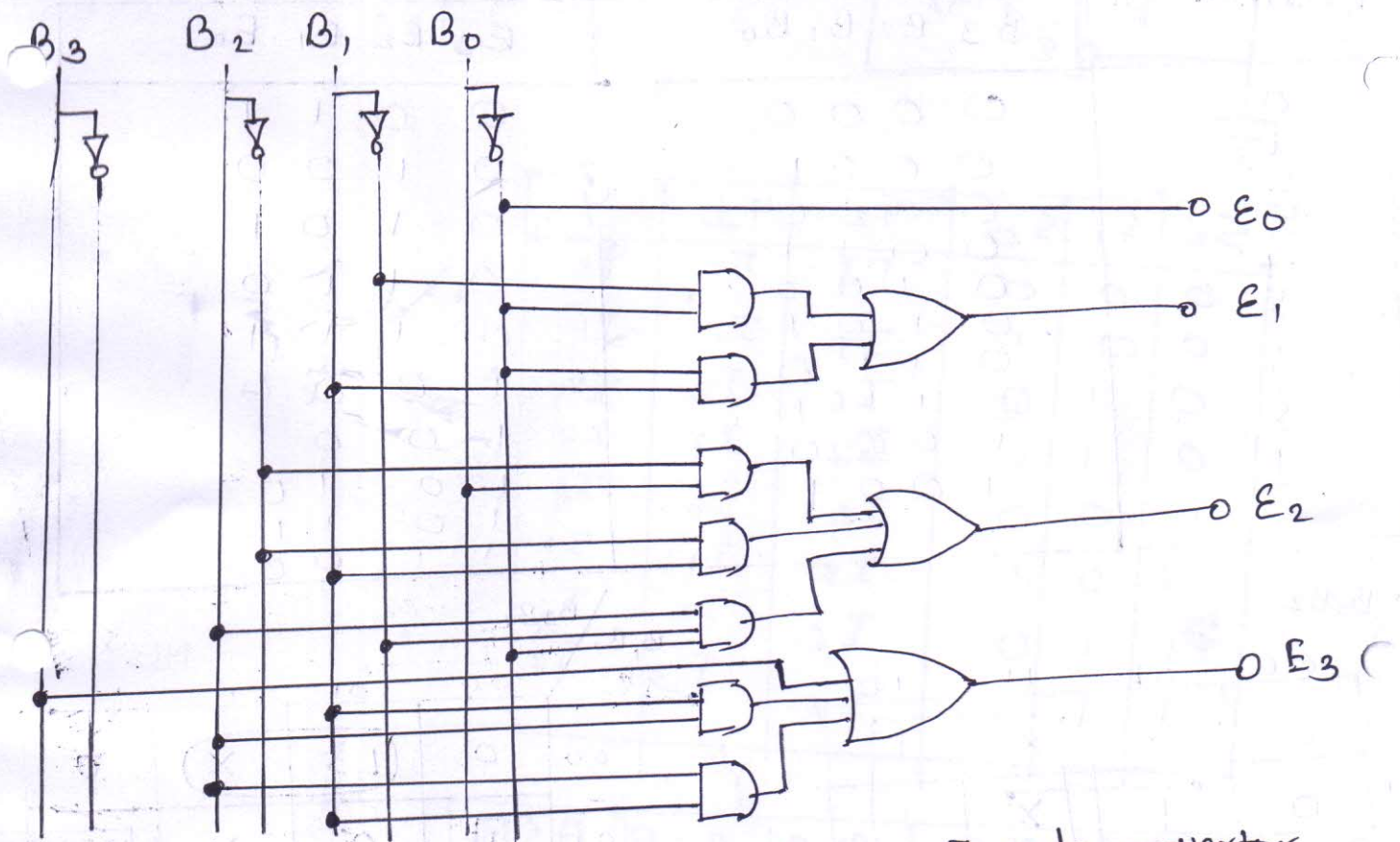
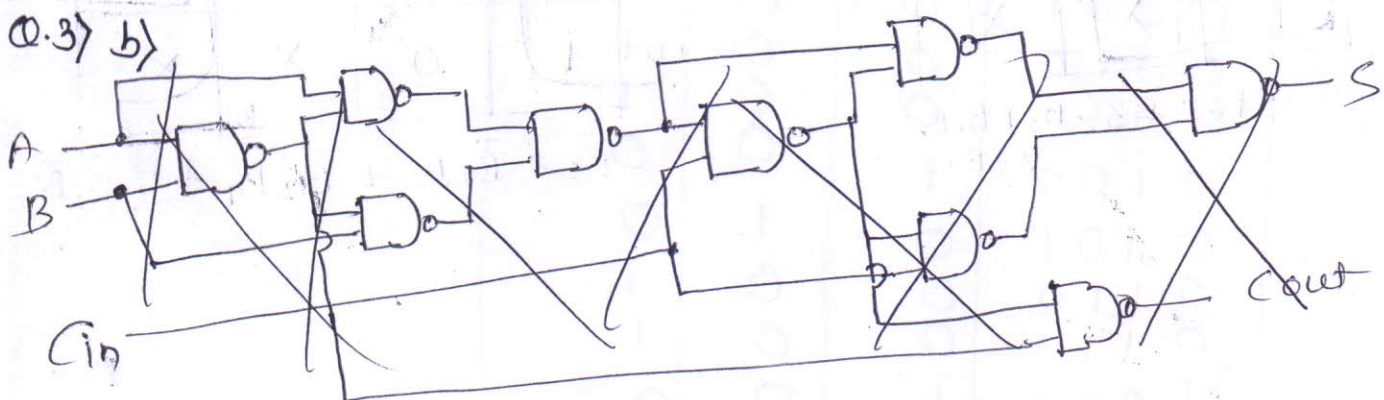
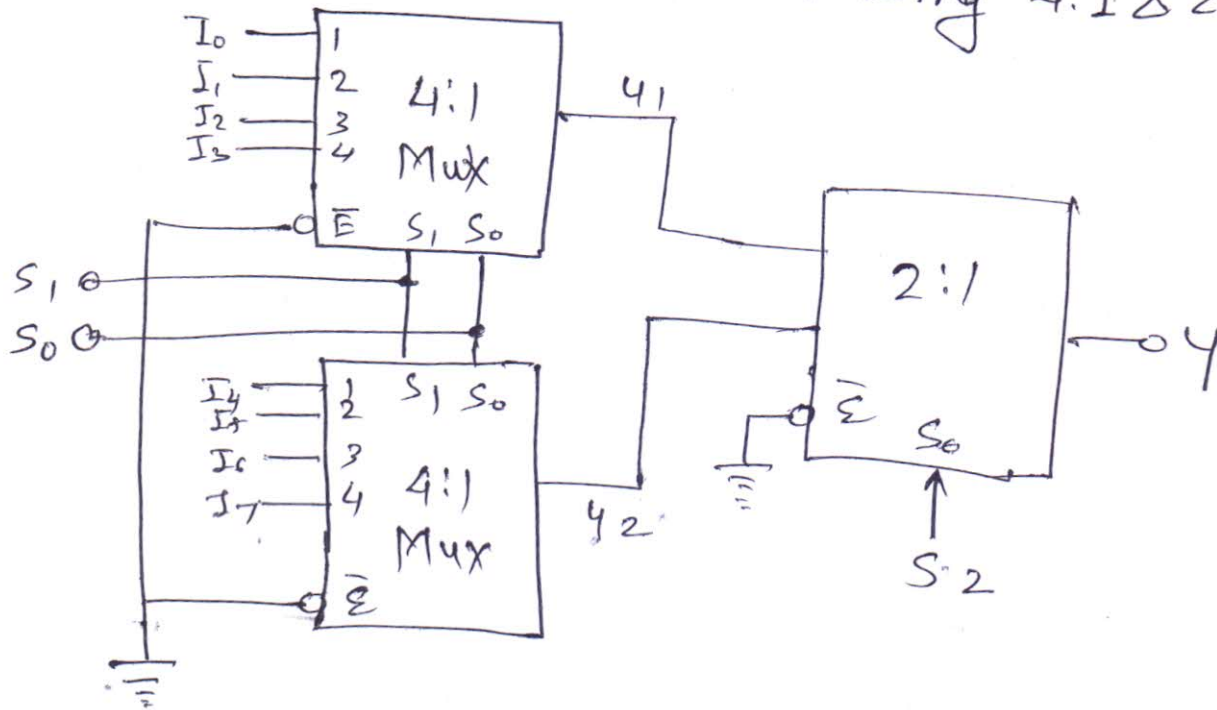


Fig: 4-Bit BCD to Excess-3 code converter



Q.3) b) Implement 8:1 Mux using 4:1 & 2:1 Mux.



S_2	S_1	S_0	Y_2	Y_1	Y
0	0	0	I_4	I_0	I_0
0	0	1	I_5	I_1	I_1
0	1	0	I_6	I_2	I_2
0	1	1	I_7	I_3	I_3
1	0	0	I_4	I_0	I_4
1	0	1	I_5	I_1	I_5
1	1	0	I_6	I_2	I_6
1	1	1	I_7	I_3	I_7

Q.3) c)

A, A_2, A_1, A_0	B, B_2, B_1, B_0	$A > B$	$A = B$	$A < B$
0	0	0	1	0
0	0	0	0	1
0	0	0	0	1
0	0	0	0	1
0	1	1	0	0
0	1	0	1	0
0	1	0	0	1
0	1	0	0	1
1	0	1	0	0
1	0	1	0	0

$A_1 A_2 B_1 B_2$	$A > B$	$A = B$	$A < B$
1 0 1 0	0	1	0
1 0 1 1	0	0	1
1 1 0 0	1	0	0
1 1 0 1	1	0	0
1 1 1 0	1	0	0
1 1 1 1	0	1	0

Map for $A > B$

$A_1 A_0$	$B_1 B_0$ 00	01	11	10
00	0	0	0	1
01	0	0	1	1
11	0	0	0	0
10	0	0	1	0

Map for $A = 0$

$A_1 A_0$	$B_1 B_0$ 00	01	11	10
00	1	0	0	0
01	0	1	0	0
11	0	0	1	0
10	0	0	0	1

Map for $A < B$

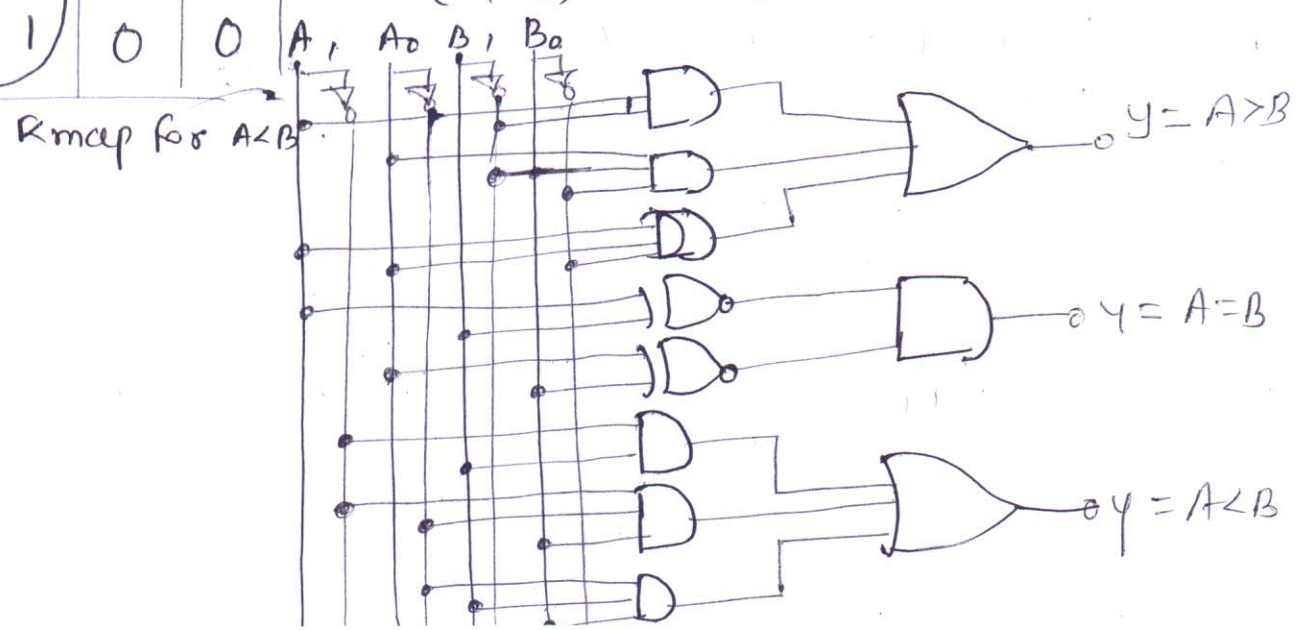
$A_1 A_0$	$B_1 B_0$ 00	01	11	10
00	0	0	0	0
01	1	0	0	0
11	1	1	0	1
10	1	1	0	0

$$(A > B) = A_1 \bar{B}_1 + A_0 \bar{B}_1 \bar{B}_0 + A_1 A_0 \bar{B}_0$$

$$(A = B) = \bar{A}_1 \bar{B}_1 \bar{A}_0 \bar{B}_0 + \bar{A}_1 A_0 \bar{B}_1 B_0 + A_1 A_0 B_1 B_0 + A_1 \bar{A}_0 B_1 \bar{B}_0$$

$$= (A_0 \odot B_0) (A_1 \odot B_1)$$

$$(A < B) = \bar{A}_1 B_1 + \bar{A}_1 \bar{A}_0 B_0 + \bar{A}_0 B_1 B_0$$



c)

A	B	D	B
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

Truth table of Subtractor using two variable.

$D = A\bar{B} + \bar{A}B$

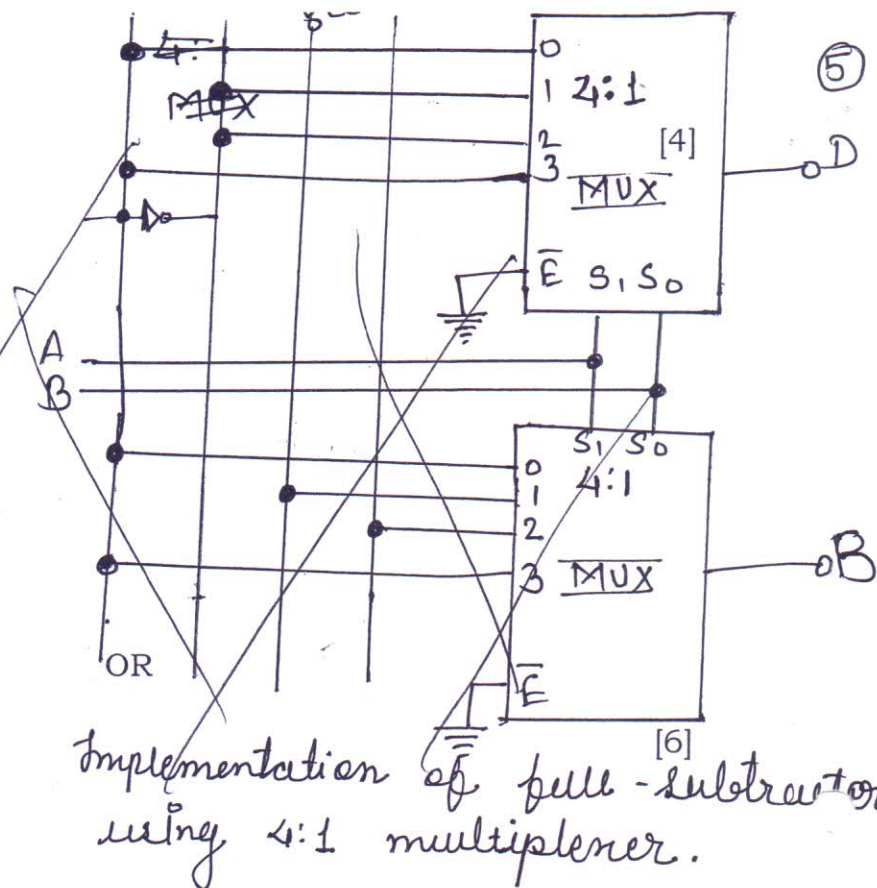
A	B	D
0	0	0
0	1	1
1	0	1
1	1	0

$D = A \oplus B$

$B = \bar{A} \cdot B$

A	B	B
0	0	0
0	1	1
1	0	0
1	1	0

$B = \bar{A} \cdot B$



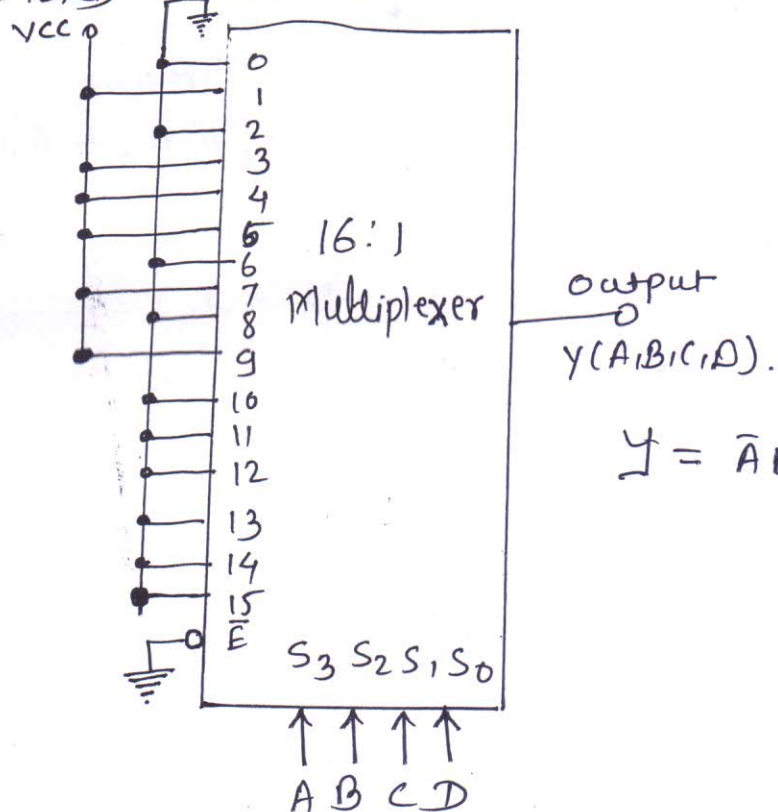
Q. 4) A)

$Y = \bar{A}\bar{B}\bar{C} + A\bar{B}\bar{C}D + \bar{A}\bar{B}D + \bar{A}CD$

$= \bar{A}\bar{B}\bar{C}(D + \bar{D}) + A\bar{B}\bar{C}D + \bar{A}\bar{B}D(C + \bar{C}) + \bar{A}CD(B + \bar{B})$

$= \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + \bar{A}\bar{B}CD + \bar{A}\bar{B}\bar{C}D + \bar{A}BCD + \bar{A}\bar{B}\bar{C}D$

$Y(A, B, C, D) = \sum m(1, 3, 4, 5, 7, 9)$



$Y = \bar{A}\bar{B}\bar{C} + A\bar{B}\bar{C}D + \bar{A}\bar{B}D + \bar{A}CD$

Q.4) b) Full-adder using 3-to-8 line decoder.
full adder has 3 i/p & 2 outputs.

[4]

A	B	C	Sum	Carry
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

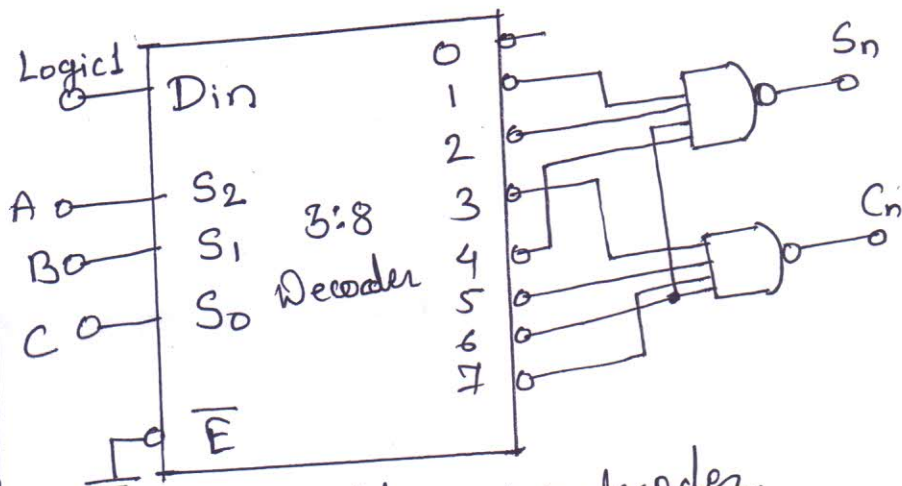


Fig: full adder using decoder.

$$S_n(A, B, C) = \sum m(1, 2, 4, 7)$$

$$C_n(A, B, C) = \sum m(3, 5, 6, 7)$$

c) Design 4:1 multiplexers using NAND gate [4] only.

4:1 multiplexer.

S_1	S_0	Y
0	0	I_0
0	1	I_1
1	0	I_2
1	1	I_3

$$Y = \bar{S}_1 \bar{S}_0 I_0 + \bar{S}_1 S_0 I_1 + S_1 \bar{S}_0 I_2 + S_1 S_0 I_3$$

$$\bar{Y} = \bar{S}_1 \bar{S}_0 \bar{I}_0 + \bar{S}_1 S_0 \bar{I}_1 + S_1 \bar{S}_0 \bar{I}_2 + S_1 S_0 \bar{I}_3$$

$$= \bar{S}_1 \bar{S}_0 \bar{I}_0 \cdot \bar{S}_1 S_0 \bar{I}_1 \cdot S_1 \bar{S}_0 \bar{I}_2 \cdot S_1 S_0 \bar{I}_3$$

(*) Course coordinator can change instructions as per course requirement

Q. 4) c) Even parity generator.

A	B	C	D	P
0	0	0	0	0
0	0	0	1	1
0	0	1	0	1
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	1
1	1	1	1	0

		AB			
CD		00	01	11	10
		0	1	0	1
00	0	0	1	0	1
01	1	1	0	1	0
11	0	1	0	0	1
10	1	0	1	1	0

$$P = \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D + A\bar{B}\bar{C}D + A\bar{B}C\bar{D} + AB\bar{C}\bar{D} + AB\bar{C}D$$

$$= \bar{A}\bar{C}(\bar{B}D + B\bar{D}) + \bar{A}C(\bar{B}\bar{D} + B\bar{D}) + A\bar{C}(\bar{B}D + \bar{B}\bar{D}) + AC(\bar{B}\bar{D} + \bar{B}D)$$

$$= \bar{A}\bar{C}(B \oplus D) + \bar{A}C(B \odot D) + A\bar{C}(B \odot D) + AC(B \oplus D)$$

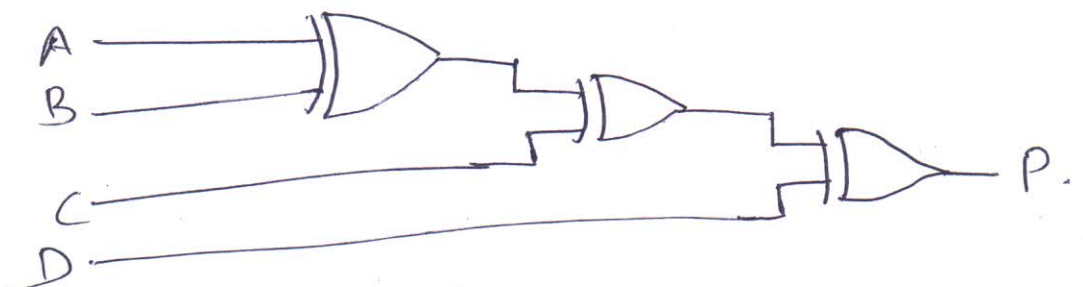
$$= (\bar{A}\bar{C} + AC)(B \oplus D) + (\bar{A}C + A\bar{C})(B \odot D)$$

$$= (A \odot C)(B \oplus D) + (A \oplus C)(B \odot D)$$

$$= (\overline{A \oplus C})(B \oplus D) + (A \oplus C)(\overline{B \oplus D})$$

$$= (A \oplus C) \oplus (B \oplus D)$$

$$P = A \oplus B \oplus C \oplus D$$



Logic Diagram.