

Total No. of Questions – [6]

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DECEMBER 2019-20 ENDSEM

S. Y. B. TECH. (E & TC) (SEMESTER -III)

COURSE NAME: Probability and Statistics

COURSE CODE: ES21182ET

(PATTERN 2018)

Time: [2 Hours]

[Max. Marks: 50]

(*) Instructions to candidates:

- 1) All questions are compulsory.
- 2) Figures to the right indicate full marks.
- 3) Use of scientific calculator is allowed.
- 4) Assume suitable data where ever required.

Q.1)	Attempt any one	
a)	The probability that India wins a cricket match against Australia is $\frac{2}{5}$. If three matches are played between the two teams, what is the probability that <ol style="list-style-type: none"> i. India win at least one match ii. India win at most one match 	[4]
b)	In a class 10 boys and 5 girls, three students are selected random one after the other. Find the probability that <ol style="list-style-type: none"> i. first two are boys and third is girl ii. first and third is of same gender and third is of opposite gender 	[4]
Q.2)	Attempt any one	
a)	A shipment of 8 similar microcomputers to a retail outlet contains 3 that are defective. If a school makes a random purchase of 2 of these computers, find and sketch the probability distribution (pdf) for number of defective pieces. Also find and sketch cdf.	[4]
b)	A continuous random variable T is used to model number of days, t, and a mosquito survives after hatching. The CDF is given by $F(t) = 1 - \frac{225}{(t+15)^2}$, $t > 0$ <ol style="list-style-type: none"> i. Find the probability that a randomly selected mosquito will die within 3 days of hatching. ii. Given that mosquito survived for 3 days, find the probability that it will survive for at least 5 more days. 	[4]

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Q.3)	Attempt any one																									
a)	Let X and Y be jointly continuous RVs. With joint Pdf $F_{XY}(X,Y) = cx^2y$ for $0 \leq y \leq x \leq 1$ i. Find constant c ii. Find marginal Pdfs $f_X(x)$ and $f_Y(y)$	[6]																								
b)	Consider the following joint distribution of X and Y <table border="1" style="margin: 10px auto;"> <tr> <td style="text-align: center;">Y X \</td> <td>-2</td> <td>-1</td> <td>4</td> <td>5</td> <td>Sum</td> </tr> <tr> <td style="text-align: center;">1</td> <td>.1</td> <td>.2</td> <td>0</td> <td>.3</td> <td>.6</td> </tr> <tr> <td style="text-align: center;">2</td> <td>.2</td> <td>.1</td> <td>.1</td> <td>0</td> <td>.4</td> </tr> <tr> <td style="text-align: center;">Sum</td> <td>.3</td> <td>.3</td> <td>.1</td> <td>.3</td> <td></td> </tr> </table> Find COV (X,Y)	Y X \	-2	-1	4	5	Sum	1	.1	.2	0	.3	.6	2	.2	.1	.1	0	.4	Sum	.3	.3	.1	.3		[6]
Y X \	-2	-1	4	5	Sum																					
1	.1	.2	0	.3	.6																					
2	.2	.1	.1	0	.4																					
Sum	.3	.3	.1	.3																						
Q.4)	Attempt any one																									
a)	1. Calculate the skew and kurtosis of an Uniform distribution, distributed over an interval [0,1] 2. Busses arrive at a stop at 15 min. interval starting at 7AM. If a passenger arrives at the stop at a random time that is uniformly distributed between 7 AM and 7:30 AM. Find probability that he waits i. <5min. ii. at least 12 min.	[6] [4]																								
b)	1. The time taken to assemble a car in a certain plant is a random variable having a normal distribution of 20 hours and a standard deviation of 2 hours. What is the probability that a car can be assembled at this plant in a period of time a) Less than 19.5 hours? b) between 20 and 22 hours? 2. The service rate at a supermarket checkout is 6 customers per hour. If the service time is exponential, find the following probabilities. a) A service is completed in 5 min. b) A customer leaves the counter more than 10 minutes after arriving (Hint: Use CDF of exponential distribution : $F(x) = 1 - e^{-x/\lambda}$, $x \geq 0$)	[6] [4]																								
Q.5)	Attempt any one																									

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	<p>a) i. Show that the Random process $X(t) = A \cos(w_c t + \phi)$, where ϕ is uniformly distributed over $[0, 2\pi]$ is wide sense stationary process [7]</p> <p>ii. The random process $X(t) = a \cos(w_c t + \phi)$, where A is uniformly distributed between $[2, 3]$ and w_c and ϕ are constants. [6]</p> <p>a. Sketch the ensemble of the random process.</p> <p>b. Justify whether it is stationary or non-stationary process</p>																	
	<p>b) i. Consider the power signal $x(t)$ with autocorrelation $R_x(\tau) = 200 \text{sinc}(200\tau)$. Find and plot. [7]</p> <p>a. Power spectral density of input</p> <p>b. The process is passed through ideal LPF with cutoff 50 Hz. Find output power.</p> <p>For each of the following functions, state whether it can be a valid PSD? Give the justification</p> <div style="display: flex; justify-content: space-around;"> <div> <p>(a) $\frac{\omega^2}{\omega^2 + 16}$</p> <p>(c) $\frac{\omega}{\omega^2 + 16}$</p> <p>(e) $\delta(\omega + \omega_0) - \delta(\omega - \omega_0)$</p> </div> <div> <p>(b) $\frac{1}{\omega^2 - 16}$</p> <p>(d) $\delta(\omega) + \frac{1}{\omega^2 + 16}$</p> <p>(f) $j[\delta(\omega + \omega_0) + \delta(\omega - \omega_0)]$</p> </div> </div> <p>[6]</p>																	
Q.6)	Attempt any one																	
	<p>a) 1. A doctor believes that the proportions of births in the country on each day of the week are equal. A random sample form 700 births in recent year is selected and the results are shown in the table below. At a significance level of 0.01, is there enough evidence to support doctor's claim?</p> <table border="1" style="margin: 10px auto;"> <tr> <td>Day</td><td>Sun</td><td>Mon</td><td>Tue</td><td>Wed</td><td>Thurs</td><td>Fri</td><td>Sat</td></tr> <tr> <td>Frequency</td><td>65</td><td>103</td><td>114</td><td>116</td><td>115</td><td>112</td><td>75</td></tr> </table> <p>2. A bank teller serves customers in a queue one by one. Suppose that the service time X_i for customer i has mean =2 and var=1. Let Y be the total time spent serving 50 customers. Find $P(90 < Y < 110)$</p> <p>[6]</p>	Day	Sun	Mon	Tue	Wed	Thurs	Fri	Sat	Frequency	65	103	114	116	115	112	75	[7]
Day	Sun	Mon	Tue	Wed	Thurs	Fri	Sat											
Frequency	65	103	114	116	115	112	75											
	<p>b) 1. The values of x and their corresponding values of y are shown in the table below</p>	[7]																

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x	0	1	2	3	4
	2	3	5	4	6
y					

a) Find the least square regression line $y = a x + b$.
b) Estimate the value of y when $x = 10$.

2. The side effects of a new drug are being tested. A sample of 565 patients yields the results below. At a significance level of 0.05, is there enough evidence to conclude that the treatment is independent of the side effects.

Result	Drug1	Drug2
Nausea	36	13
No nausea	254	262

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