

G.R. No. 





paper code: P119-111 CT1

OCTOBER 2019 / INSEM (T1)  
 F. Y. M. TECH. (STRUCTURES) (SEMESTER - I)  
 COURSE NAME: THEORY OF ELASTICITY  
 COURSE CODE: CVPB11181  
 (PATTERN 2018:R1)

Time: [1 Hour]

[Max. Marks: 20]

(\*) Instructions to candidates:

- 1) Answer Q.1 OR Q.2, Q.3 OR Q.4
- 2) Figures to the right indicate full marks.
- 3) Use of scientific calculator is allowed
- 4) Use suitable data where ever required

Q.1) Derive the equilibrium equations for a three dimensional stress system subjected to direct stress ( $\sigma$ ) and shearing stress ( $\tau$ ) [ 10 marks]

OR

Q.2) a) An elastic body under the action of external forces has the displacement field given by [4marks]

$$D = (2x^2 + y^2) i + (5z - y) j + (3x + y^2) k$$

Evaluate the component of strain at a point (3,1,2)

Q.2) b) Determine whether the following stress components satisfy equilibrium equations or not, at the point (1,-1, 2). If not, determine the suitable body force required at this point so that these stress components are under equilibrium. [6 marks]

$$\sigma_x = 3xy^2z + 2x$$

$$\sigma_y = 5xyz + 3y$$

$$\sigma_z = x^2y + y^2z$$

$$\tau_{xy} = 0$$

$$\tau_{yz} = \tau_{xz} = 3xy^2z + 2xy$$

Q.3) a) The components of strain at a point in a body are as follows: [4 marks]

$$\epsilon_x = C_1 (x^2 + y^2) z \quad \epsilon_y = x^2 z \quad \gamma_{xy} = 2 C_2 xyz$$

where  $C_1, C_2$  are constants. Check whether the strain field is compatible one?

Q.3) b) Following are the principal stress at a point in a stressed material. Taking  $E = 210$  KN/mm<sup>2</sup> and  $\mu = 0.3$ , calculate the volumetric strain and Lamé's Constant. [6 marks]

$$\sigma_x = 200 \text{ N/mm}^2,$$

$$\sigma_y = 150 \text{ N/mm}^2 \text{ and}$$

$$\sigma_z = 120 \text{ N/mm}^2$$

OR

Q.4) Derive Beltrami-Michell compatibility equations for Plane Stress Problem.

[10 marks]