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PAPER CODE	VIII-2013 (RE)
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DECEMBER 2021 (INSEM+ ENDSEM) EXAM

F.Y. B. TECH. (SEMESTER - I)

COURSE NAME: CALCULUS

COURSE CODE: ES10201B

(PATTERN 2020)

Time: [2Hr]

[Max. Marks: 60]

(*) Instructions to candidates:

- 1) Figures to the right indicate full marks.
- 2) Use of scientific calculator is allowed
- 3) Use suitable data where ever required

Q.1 Solve the following

i) If $f(x, y) = \frac{\sin(xy^2 + y)}{x^2 + 1}$ then the value of $\frac{\partial f}{\partial y} =$ [2]

- A) 0 B) 1 C) -1 D) ∞

ii) If $z^3 - zx - y = 3$ then the value of $\frac{\partial z}{\partial x} =$ [2]

- A) $\frac{z}{3z^2 + 1}$ B) $\frac{z}{3z^2 - 1}$ C) $\frac{1}{3z^2 + 1}$ D) $\frac{1}{3z^2 - 1}$

iii) If $u = \log(x^2 + y^2)$ then ... [2]

- A) $u_{xy} = u_{yx}$ B) $u_{xy} = \frac{1}{u_{yx}}$
C) $u_{xy} = -u_{yx}$ D) $u_{xy} = 1 + u_{yx}$

iv) If $u = \sin^{-1}(x^2 + y^2 + z^2)$ then $xu_x + yu_y + zu_z =$ [2]

- A) $2 \cos u$ B) $2 \sin u$ C) $2 \cot u$ D) $2 \tan u$

v) If $x = u \cos v$, $y = u \sin v$ then, $\frac{\partial(x, y)}{\partial(u, v)} =$ [2]

- A) u B) $\frac{1}{u}$ C) u^2 D) $\frac{1}{u^2}$

vi) If $x = e^u \cos v$, $y = e^u \sin v$ then, $\frac{\partial(x, y)}{\partial(u, v)} \cdot \frac{\partial(u, v)}{\partial(x, y)} =$ [2]

- A) 0 B) 1 C) 2 D) 3

vii) If $u = 2xy$, $v = x^2 - y^2$ where $x = r \cos \theta$, $y = r \sin \theta$ then, $\frac{\partial(u, v)}{\partial(r, \theta)} =$ [2]

- A) $-4r^2$ B) $-\frac{1}{4r^2}$ C) $-4r^3$ D) $-\frac{1}{4r^3}$

viii) If $f(x, y) = x^3 y^2 (12 - x - y)$ then the maximum value occurs at [2]
A) (4, 6) B) (-4, -6) C) (-6, -4) D) (6, 4)

ix) If $f(x, y) = xy + a^3 \left(\frac{1}{x} + \frac{1}{y} \right)$ then the stationary points are: [2]

- A) $(-a, -a)$ B) (a, a) C) $(-a, a)$ D) $(a, -a)$

x) If there is an error of 1% while measuring both major and minor axes, then the % error in the area of an ellipse is [2]

- A) 2% B) 4% C) 6% D) 8%

xi) $\int_0^\pi \sin^7 x \, dx =$ [2]

- A) 0 B) $\frac{32\pi}{35}$ C) $\frac{32}{35}$ D) $\frac{35}{32}$

xii) $\int_{-\pi}^\pi \sin^4 x \cos^2 x \, dx =$ [2]

- A) $\frac{\pi}{2}$ B) $\frac{\pi}{4}$ C) $\frac{\pi}{6}$ D) $\frac{\pi}{8}$

xiii) $\Gamma(3.5) =$ [2]

- A) $\frac{15\pi}{8}$ B) $\frac{15\sqrt{\pi}}{8}$ C) $\frac{35\pi}{4}$ D) $\frac{35\sqrt{\pi}}{4}$

xiv) $\int_0^1 x^{-3/4} (1-x)^{-1/4} \, dx =$ [2]

- A) $\frac{\pi}{2}$ B) $\frac{\pi}{4}$ C) $\frac{\pi}{6}$ D) $\frac{\pi}{8}$

xv) The value of a_0 in the Fourier series of $f(x) = x \sin x$ in $0 < x < 2\pi$ is [2]

- A) 0 B) 1 C) 2 D) -2

Q.2 Solve any two out of three

a) Solve: $\frac{dy}{dx} = \frac{5-3x-2y}{2x+3y-5}$ [5]

b) Solve: $\frac{dz}{dx} + \frac{z}{x} \log z = \frac{z}{x^2} (\log x)^2$ [5]

c) If the temperature of a body drops from 100°C to 60°C in one minute when the temperature of the surrounding is 20°C . What will be the temperature at the end of the second minute? [5]

Q.3 Solve any two out of three

a) Trace the curve: $y^2(x-a) = a^2(2a-x)$ [5]

b) Trace the curve: $r = a(1 + \cos \theta)$ [5]

c) Find the whole length of the loop of the curve: $3y^2 = x(x-1)^2$ [5]

Q.4 Solve any two out of three

a) Evaluate:

[5]

$$\int_0^1 \int_x^{\sqrt{x}} (x^2 + y^2) dx dy$$

b) Evaluate:

[5]

$$\int_0^1 \int_0^{1-x} \int_0^{x+y} e^z dx dy dz$$

c) Find the total area of the curve, $r = a(1 + \cos \theta)$

[5]